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Introduction

t is a great pleasure to introduce the latest issue of the Research Insights supplement to AsianInvestor. We begin by introducing a new approach to equity investing termed 'smart factor investing.' The results suggest that smart factor indices lead to considerable improvements in risk-adjusted performance. These smart factor indices are not the end point for investing in equities in a smart way, but instead the starting point, ingredients to construct smart beta allocation solutions while respecting risk objectives that can be expressed in absolute or relative terms. This first article provides a panorama of solutions that have been the subject of a considerable research effort conducted by EDHEC-Risk

Turning to risk allocation with smart factor indices, we examine a case study with factor exposure constraints in a second article. We show that it is possible to perform risk parity in the long-only world, i.e. to have an exposure that is equal in terms of risk factors rewarded over the long term without necessarily having pure or orthogonal factors that are impossible to obtain in the long-only space.

Institute with the support of Amundi ETF & Indexing.

As part of our solutions for allocating to smart beta, we find that value can be added through relative Equal Risk Contribution and relative Global Minimum Variance at the allocation stage, for investors with a tracking error budget. As a result, extremely substantial levels of risk-adjusted outperformance (information ratios) can be achieved even in the absence of views on factor returns

The question that all investors raise for an innovative solution is its investability. The objective of the fourth article is to describe how to ensure that smart beta indices are investable by managing turnover control and capacity constraints.

The results we present are sufficiently impressive for investors to raise the question of their robustness. Our results show that single factor indices have a high degree of relative robustness, but they are not robust in absolute terms. Multi-beta allocations, on the other hand, are highly robust in absolute terms.

To conclude this special issue on smart beta, we provide a brief overview of equity factor index offerings from major index providers. Factor indices aim to provide explicit exposure to a common risk factor to harvest its long-term risk premia.

We hope you will find the articles on smart beta in the supplement informative, relevant and instructive. We would like to extend our thanks to AsianInvestor for their collaboration on this supplement, which now enters its third year. We hope that the supplement will be providing practical research insights for Asian investment professionals for many years to come.

Noël Amenc

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www.asianinvestor.net March 2015 AsianInvestor

Smart Factor Investing

By Noël Amenc, Romain Deguest, Felix Goltz, Ashish Lodh, Lionel Martellini and Eric Shirhin

We focus on four well-known

his article argues that current smart beta investment approaches only provide a partial answer to the main shortcomings of capitalisation-weighted (cap-weighted) indices, and introduces a new approach to equity investing referred to as smart factor investing. It provides an assessment of the benefits of simultaneously addressing the two main shortcomings of cap-weighted indices, namely their undesirable factor exposures and their heavy concentration, by constructing factor indices that explicitly seek exposures to rewarded risk factors while diversifying away unrewarded risks. The results we obtain suggest that such smart factor indices lead to considerable improvements in risk-adjusted performance.

For long-term US data, smart factor indices for a range of different factor tilts roughly double the Sharpe ratio of the broad cap-weighted index. Outperformance of such indices persists at levels ranging from 2.92% to 4.46%, even when assuming unrealistically high transaction costs. Moreover, by providing explicit tilts to consensual factors, such indices improve upon many current smart beta offerings where, more often than not, factor tilts result as unintended consequences of ad hoc methodologies. In fact, our research shows that by using consensual results from asset pricing theory concerning both the existence of factor premia and the importance of diversification, it is possible to go beyond existing smart beta approaches which provide partial solutions by only addressing one of these

Designing efficient and investable proxies for risk premia

rewarded factors - the Size and Value factors (Fama and French (1993)), the Momentum factor (Carhart (1997)) and the Low Volatility factor (Ang et al. (2006, 2009)). For each rewarded factor, we introduce a corresponding smart factor index, which can be regarded as an efficient investable proxy for a given risk premium. In a nutshell, a risk premium can be thought of as a combination of a risk (exposure) and a premium (to be earned from the risk exposure). Smart factor indices have been precisely engineered to achieve a pronounced factor tilt emanating from the stock selection procedure (relevant risk exposure), as well as high Sharpe ratio emanating from the efficient diversification of unrewarded risks related to individual stocks (fair reward for the risk exposure). The access to the fair reward for the given risk exposure is obtained through a well-diversified, also known as smart-weighted, portfolio, as opposed to a concentrated cap-weighted portfolio, of the selected stocks so as to ensure that the largest possible fraction of individual stocks' unrewarded risks is eliminated.

The results in Exhibit A confirm that the combination of relevant security selection and appropriate weighting schemes in a two-step process leads to substantial improvements in risk-adjusted performance with respect to the use of a standard cap-weighted index, which typically implies an inefficient set of factor exposures and an excess of unrewarded risk.

On the one hand, starting with a focus on the systematic risk exposure, we find that a higher Sharpe ratio can be achieved with the same weighting scheme, here a cap-weighting scheme, for stocks selected on the basis of their loadings on the value, size, momentum and low volatility factors, compared to the case where the full universe is held in the form of a cap-weighted portfolio.

The results we obtain, reported in Exhibit A, show that while the Sharpe ratio of the cap-weighted index is 0.24 on the sample period, it reaches values as high as 0.39 for a mid cap stock selection, 0.30 for a high momentum stock selection, 0.29 for a low volatility stock selection or 0.35 for a value stock selection. These results suggest that a systematic attempt to harvest equity risk premia above and beyond broad market exposure leads to additional risk-adjusted performance. It should be noted at this stage that substantially higher levels of max Drawdown are incurred for the mid cap and value selections, confirming that the reward harvested through the factor exposure is a compensation for a corresponding increase in risk. In contrast, we note that high momentum and low volatility selections lead to lower levels of max Drawdown compared to the no selection case, suggesting that the excess performance earned on these two factors has at best a behavioural explanation, and is not necessarily related to an increased riskiness.

On the other hand, shifting to the management of specific risk exposures, we find that even higher levels of Sharpe ratio can be achieved for each selected factor exposure through the

Such indices improve upon many current smart beta offerings where, more often than not, factor tilts result as unintended consequences of ad hoc methodologies'

Exhibit A: Performance comparison of USA Cap Weighted Factor Indices and USA Multi-Strategy Factor Indices

The exhibit shows the absolute performance, relative performance, and risk indicators for Cap Weighted (CW) Factor Indices and Multi-Strategy Factor Indices for four factor tilts – mid cap, high momentum, low volatility, and value. The complete stock universe consists of the 500 largest stocks in the USA. The benchmark is the cap-weighted portfolio of the full universe. The yield on secondary market US Treasury Bills (3M) is the risk-free rate. The return-based analysis is based on daily total returns from 31/12/1972 to 31/12/2012 (40 years). All weight based statistics are average values across 160 quarters (40 years) from 31/12/1972 to 31/12/20.

| | | Mid Ca | | High Mo | mentum | Low Volatility | | Value | |
|----------------------------|-------------|--------|----------------------------------|---------|----------------------------------|----------------|----------------------------------|--------|----------------------------------|
| | Broad CW | CW | Diversified Multi Strategy | CW | Diversified Multi Strategy | CW | Diversified Multi Strategy | CW | Diversified Multi Strategy |
| Ann Returns | 9.74% | 12.54% | 14.19% | 10.85% | 13.30% | 10.09% | 12.64% | 11.78% | 14.44% |
| Ann Volatility | 17.47% | 17.83% | 16.73% | 17.60% | 16.30% | 15.89% | 14.39% | 18.02% | 16.55% |
| Sharpe Ratio | 0.24 | 0.39 | 0.52 | 0.30 | 0.48 | 0.29 | 0.50 | 0.35 | 0.54 |
| Historical Daily 5% VaR | 1.59% | 1.60% | 1.50% | 1.64% | 1.50% | 1.42% | 1.28% | 1.59% | 1.47% |
| Max Drawdown | 54.53% | 60.13% | 58.11% | 48.91% | 49.00% | 50.50% | 50.13% | 61.20% | 58.41% |
| Ann Excess Returns | - | 2.80% | 4.45% | 1.10% | 3.56% | 0.35% | 2.90% | 2.04% | 4.70% |
| Ann Tracking Error | - | 5.99% | 6.80% | 3.50% | 4.88% | 4.44% | 6.17% | 4.74% | 5.82% |
| 95% Tracking Error | - | 9.39% | 11.56% | 6.84% | 8.58% | 9.20% | 11.53% | 8.72% | 10.14% |
| Information Ratio | - | 0.47 | 0.66 | 0.32 | 0.73 | 0.08 | 0.47 | 0.43 | 0.81 |

use of a well-diversified weighting scheme, which we take to be an equally-weighted combination of 5 popular smart weighting schemes¹. Thus, the Sharpe ratio of the so-called *diversified multi-strategy* combination reaches 0.52 for mid cap stocks, 0.48 for high momentum stocks, 0.50 for low volatility stocks and 0.54 for value stocks.

These results suggest that multistrategy factor-tilted indices obtain the desired factor tilts without undue concentration, which provides an explanation for their superior riskadjusted performance with respect to the cap-weighted combination of the same selection of stocks.

Overall, it appears that the combined effects of a rewarded factor exposure ensured by a dedicated proper security selection process and an efficient harvesting of the associated premium through improved portfolio diversification leads to a Sharpe ratio improvement of around 100% compared to the broad cap-weighted index.

Risk allocation with smart factor indices

Once a series of smart factor indices have been developed for various regions of the equity universe, they can be used as attractive building blocks in the design of an efficient allocation to these multiple risk premia.

In an attempt to identify, and analyse the benefits of, the possible approaches to efficient risk allocation across the various smart factor indices, we identify four main dimensions that can be taken in consideration when designing a sophisticated allocation methodology (see Exhibit B).

The first, and arguably most important, dimension relates to whether risk is defined by the investor from an absolute perspective in the absence of a benchmark, or whether it is instead defined in relative terms with respect to an existing benchmark, which is more often than not a cap-weighted index. In the former situation, one would use volatility as a relevant risk measure, while tracking error with respect to the cap-weighted index would instead be used in the latter case.

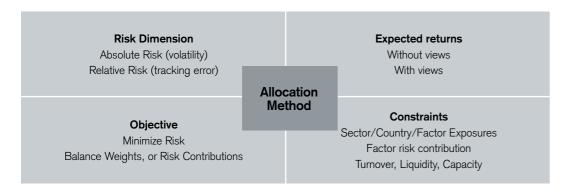
The second dimension concerns whether one would like to incorporate views regarding factor returns in the optimisation process. While additional benefits can be obtained from the introduction of views on factor returns at various points of the business cycle, we focus in what follows only on approaches that are solely based on risk parameters, which are notoriously easier

to estimate with a sufficient degree of robustness and accuracy (Merton (1980)). The third dimension is related to the objective of the allocation procedure. Indeed, there are several possible targets for the design of a well-diversified portfolio of factor exposure, depending upon whether one would like to use naive approaches (equal dollar allocation or equal risk allocation) or scientific approaches based on minimising portfolio risk (volatility in the absolute return context or tracking error in the relative return context). The fourth and last dimension related to the presence of various forms of constraints such as minimum/maximum weight constraints, turnover constraints, or factor exposure constraints, which are obviously highly relevant in the context of risk factor allocation.

To illustrate the benefits of an efficient allocation to smart factor indices, we consider a second dataset over the 10-year period from 31-Dec-2003 to 31-Dec 2013 using five sub-regions of the global developed universe, namely, US, UK, Dev. Europe Ex UK, Japan, Dev. Asia Pacific Ex Japan. Using the four smart multistrategy indices as proxies for the value, size, momentum and volatility rewarded tilts in each region, we obtain a total of (5x4) 20 constituents.

Diversified Multi-Strategy weighting is an equal-weighted combination of the following five weighting schemes – Maximum Deconcentration, Diversified Risk Weighted, Maximum Decorrelation, Efficient Minimum Volatility and Efficient Maximum Sharpe Ratio (see www.scientificbeta. com for more details).

Exhibit B - The various dimensions of allocation methodologies across assets or risk factors



Absolute return perspective

We start from the absolute return perspective and consider in Exhibit C five allocation strategies to the 20 aforementioned smart factor indices – an equal dollar contribution portfolio (denoted by Multi Beta EW Allocation), an equal risk contribution portfolio (denoted by Multi Beta ERC Allocation), and then a global minimum variance portfolio (denoted by Multi Beta GMV Allocation). Given that these allocation strategies lead in general to concentrated factor exposures (for example the minimum variance portfolio heavily loads on the low volatility factor indices

in each region), we also introduce factor risk parity constraints – that is we restrict our analysis to portfolios such that each one of the four factors has the same contribution to the portfolio volatility. More precisely we consider a global minimum variance portfolio subject to factor risk parity constraints (denoted by Multi Beta GMV- Fact. Allocation), as well as a maximum deconcentration portfolio subject to factor risk parity constraints (denoted by Multi Beta MDecon - Fact. Allocation), a portfolio which can be regarded as the closest approximation to an equallyweighted portfolio that satisfies the

factor risk parity constraints2.

We note that the GMV allocation process leads to the lowest volatility, as expected. When analysing the performances in terms of bull versus bear market regimes (defined as positive versus negative returns for the capweighted index), we observe that the addition of risk parity constraints to the GMV allocation tends to stabilise the returns across market conditions. For example, in the absence of a factor risk parity constraint, the GMV allocation leads to a massive outperformance of 11.94% with respect to the cap-weighted index in bear markets, which is due to

Exhibit C - Multi Beta Allocations across Smart Factor Indices (Developed Universe).

The graph shows the allocations of the EW, ERC, GMV under geographical constraints, and both the maxdeconcentration and GMV Diversified Multi-Strategy indices under geographical and risk parity constraints, invested in the 20 Diversified Multi-Strategy indices with stock selection based on mid cap, momentum, low volatility, and value in the five sub-regions – US, UK, Dev. Europe Ex UK, Japan and Pacific Asia Ex Japan. The period goes from 31-December-2003 to 31-December-2013.

| | | Diversified Multi-Strategy | | | | | | | |
|-----------------------|--------------------|--------------------------------|---------------------------------|---------------------------------|---|--------------------------------------|--|--|--|
| Developed (2004-2013) | CW (All Stocks) | Multi Beta EW Allocation | Multi Beta ERC Allocation | Multi Beta GMV Allocation | Multi Beta MDecon-Fact Allocation | Multi Beta GMV-Fact Allocation | | | |
| Ann Returns | 7.80% | 11.37% | 11.07% | 10.57% | 11.17% | 10.88% | | | |
| Ann Volatility | 17.09% | 15.32% | 14.33% | 12.84% | 17.23% | 17.21% | | | |
| Sharpe Ratio | 0.36 | 0.64 | 0.66 | 0.70 | 0.56 | 0.54 | | | |
| Max Drawdown | 57.13% | 54.40% | 51.82% | 45.07% | 55.22% | 55.32% | | | |
| Excess Returns | - | 3.56% | 3.27% | 2.76% | 3.37% | 3.07% | | | |
| Tracking Error | - | 6.75% | 7.51% | 6.36% | 3.08% | 3.34% | | | |
| 95% Trk Error | - | 13.84% | 14.89% | 11.85% | 5.19% | 5.55% | | | |
| Information Ratio | - | 0.53 | 0.44 | 0.43 | 1.09 | 0.92 | | | |
| Outperf Prob (3Y) | - | 98.36% | 89.34% | 89.07% | 100.00% | 100.00% | | | |
| Max Rel Drawdown | - | 6.35% | 9.54% | 13.10% | 4.03% | 5.47% | | | |
| Ann. Rel. Ret. Bull | - | 2.50% | 0.48% | -3.90% | 3.81% | 3.18% | | | |
| Ann. Rel. Ret. Bear | - | 4.65% | 6.74% | 11.94% | 2.50% | 2.66% | | | |

² So as to avoid introducing overly strong biases in country exposures, we also introduce a set of constraints dedicated to ensuring that each one of the five regions is not too strongly under- or over-represented with respect to its market capitalisation in the cap-weighted global developed index.

the almost exclusive domination of the low volatility factor, with a defensive bias that proves extremely useful in such market conditions.

On the other hand, the relative return in bull markets is negative at -3.90% due to the performance drag associated with exclusively holding defensive equity exposure in bull market conditions. In this context, one key advantage of the introduction of factor risk parity constraints is that it leads to a much more balanced return profile across market conditions with positive outperformance in both bear and bull markets (at 2.66% and 3.18% respectively).

We also find that the introduction of factor risk parity constraints has led to a substantial improvement in information ratios with an information ratio above 1 for the Max-Deconcentration allocation under risk parity constraints. Interestingly we note that the introduction of factor risk parity constraints leads to 100% outperformance probabilities over a three-year horizon. Overall, all tested strategies lead to extremely substantial levels of outperformance with respect to the cap-weighted index, with excess returns ranging between 276 and 356 basis points per annum.

Relative return perspective

It is often the case that investors maintain the cap-weighted index as a benchmark, which has the merit 'All tested
strategies lead
to extremely
substantial levels
of outperformance
with respect to
the cap-weighted
index'

of macro-consistency and is wellunderstood by all stakeholders. In this context, a multi-smart beta solution can be regarded as a reliable cost-efficient substitute to expensive active managers, and the most relevant perspective is not an absolute return perspective, but a relative return perspective, with respect to the cap-weighted index.

In what follows, we focus on two approaches, a naive diversification approach leading to a relative equal risk allocation (R-ERC) portfolio, which focuses on equalising the contribution of the smart factor-tilted indices to the portfolio tracking error, and a scientific diversification approach leading to a relative global minimum variance (R-GMV) portfolio, also known as minimum tracking error portfolio, which focuses on minimising the variance of the portfolio relative returns with respect to the capweighted index.

From the results reported in Exhibit D, we note that the focus on relative return leads to lower tracking error levels compared to the portfolios that had an absolute return focus. For example, the ex-post tracking error is around 2.50% for these two portfolios (2.43% for the relative minimum variance portfolio and 2.56% for the relative equal risk contribution portfolio). Such low tracking error levels, associated with substantial outperformance (more than 300 basis points per annum

Exhibit D - Relative ERC and GMV Allocation across Smart Factor Indices (Developed Universe)

The table compares performance and risk of Scientific Beta Diversified Multi-Strategy indices converted in US dollars. We look at relative ERC and relative GMV allocations invested in the 20 Diversified Multi-Strategy indices with stock selection based on mid cap, momentum, low volatility, and value in the five sub-regions – US, UK, Dev. Europe Ex UK, Japan and Pacific Asia Ex Japan. The period goes from 31-December-2003 to 31-December-2013.

| Developed | | Diversified Multi-Strategy | | | |
|---------------------------------------|-----------------|---------------------------------------|------------------------------------|--|--|
| Developed (2004-2013) (All Stocks) | CW (All Stocks) | Multi Beta Relative ERC Allocation | Multi Beta Relative GMV Allocation | | |
| Ann Returns | 7.80% | 10.92% | 9.96% | | |
| Ann Volatility | 17.09% | 16.10% | 16.64% | | |
| Sharpe Ratio | 0.36 | 0.58 | 0.50 | | |
| Max Drawdown | 57.13% | 54.14% | 55.50% | | |
| Excess Returns | - | 3.12% | 2.15% | | |
| Tracking Error | - | 2.56% | 2.43% | | |
| 95% Trk Error | - | 4.70% | 4.27% | | |
| Information Ratio | - | 1.22 | 0.88 | | |
| Outperf Prob (3Y) | - | 100.00% | 89.34% | | |
| Max Rel Drawdown | - | 5.10% | 4.95% | | |
| Ann. Ret. Bull | - | 31.38% | 31.02% | | |
| Ann. Ret. Bear | - | -25.25% | -26.93% | | |

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Well-rewarded factor-tilted indices constitute attractive building blocks for the design of an improved equity portfolio'

for the R-ERC portfolio), eventually leads to exceedingly high information ratios. In particular, the relative ERC has an information ratio of 1.22, which is the highest level among all portfolio strategies tested so far, with an outperformance probability of 100% over any given three-year investment horizon during the same period.

Conclusion: from cap-weighted indices to smart factor indices

We find that well-rewarded factor-tilted indices constitute attractive building blocks for the design of an improved equity portfolio. First-generation smart beta investment approaches only provide a partial answer to the main shortcomings of cap-weighted indices. Multi-Strategy factor indices, which diversify away unrewarded risks and seek exposure to rewarded risk factors, address the two main problems of cap-weighted indices (their undesirable factor exposures and their heavy concentration) simultaneously.

The results suggest that such Multi-Strategy factor indices lead to considerable improvements in risk-adjusted performance. For long-term US data, smart factor indices for a range of different factor tilts roughly double the Sharpe ratio of the broad cap-weighted index. Moreover, outperformance of such indices persists at levels ranging from 2.92% to 4.46%, even when assuming unrealistically high transaction costs. The outperformance of Multi-Strategy factor indices over cap-weighted factor indices is observed for other developed stock markets

as well. By providing explicit tilts to consensual factors, such indices improve upon many current smart beta offerings where, more often than not, factor tilts result as unintended consequences of *ad boc* methodologies.

Moreover, additional value can be added at the allocation stage, where the investor can control for the dollar and risk contributions of various constituents or factors to the absolute (volatility) or relative risk (tracking error) of the portfolio. As a result, extremely substantial levels of risk-adjusted outperformance (information ratios) can be achieved even on the absence of views on factor returns. The portfolio strategies we have presented in this publication can be regarded as robust attempts at generating an efficient strategic factor allocation benchmark in the equity space. Obviously, active portfolio managers may generate additional value on top of this efficient benchmark by incorporating forecasts of factor returns at various points of the business cycle in the context of tactical factor allocation decisions.

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References

- Amenc, N., R. Deguest, F. Goltz, A. Lodh, L. Martellini and E. Shirbini. June 2014. Risk Allocation, Factor Investing and Smart Beta: Reconciling Innovations in Equity Portfolio Construction. EDHEC-Risk Publication produced with the support of Amundi ETF & Indexing.
- Ang, A., R. Hodrick, Y. Xing and X. Zhang. 2009. The Cross-Section of Volatility and Expected Returns. *Journal of Finance* 61(1): 259-299
- Ang, A., Hodrick, Y. Xing and X. Zhang. 2009. High Idiosyncratic Volatility and Low Returns: International and Further U.S. Evidence. Journal of Financial Economics 91: 1-23.
- Carhart, M.M. 1997. On Persistence in Mutual Fund Performance. *Journal of Finance* 52(1): 57-82.
- Fama, E. and K. French. 1993. Common Risk Factors in the Returns on Stocks and Bonds. *Journal of Financial Economics* 33(1): 3-56.
- Merton, R. 1980. On Estimating the Expected Return on the Market: An Exploratory Investigation. *Journal of Financial Economics* 8: 323-361.



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How to Perform Risk Allocation with Smart Factor Indices

By Noël Amenc, Romain Deguest, Felix Goltz and Ashish Lodh

n the context of generating a "smart" (meaning *efficient*) allocation to smart factor indices, a natural first, albeit naïve, approach, consists in forming an equally-weighted portfolio of the selected smart factor indices, in this case the indices that serve as proxies for the value, small cap, momentum and low volatility risk premia.

While an equally-weighted scheme is the simplest approach one can use, it is likely that the use of more sophisticated weighting schemes could add additional value, in particular when it comes to the management of the risks relative to the CW benchmark. We shall sequentially consider in what follows the absolute return approach both with and without factor risk parity/ budgeting constraints. We consider naïve approaches to diversification (maximum deconcentration in terms of dollar or risk contributions) and scientific approaches (minimum risk from the absolute return perspective). One of the important aims of this article will also be to show that it is possible to perform risk parity in the long-only world, i.e. to have an exposure that is equal in terms of risk factors rewarded over the long term without necessarily having pure or orthogonal factors that are impossible to obtain in the long-only space. This point is all the more important in that often, under the pretext of purity, investors choose excessively concentrated factor indices that contribute neither purity nor diversification and therefore have a fairly low risk-adjusted return. Our argument here is that by using well-diversified investable proxies for each factor (the Scientific Beta smart factor indices), it is possible to implement high-performance allocation between these indices while respecting factor risk parity constraints.

All these methodologies will be implemented without any active views (expected return forecasts) on constituents or factors; they generate portfolios that can be regarded as attractive starting points, with very substantial risk-adjusted outperformance benefits with respect to cap-weighted indices, to which additional benefits could be added by asset managers possessing skills for actively timing factor exposures.

It is likely that
the use of more
sophisticated
weighting schemes
could add additional
value

The Developed dataset extends over the 10-year period from 31-December-2003 to 31- December-2013 and uses 5 subregions of the global developed universe: US, UK, Developed Europe ex UK, Japan, and Asia Pacific ex Japan. Using four smart multi-strategy indices as proxies for the value, size, momentum, and volatility-rewarded tilts in each sub-region, we obtain a total of 5x4 = 20 constituents. For US illustrations, long-term (40-year) data from 31-December-1973 to 31-December-2013 is used for the four smart multi-strategy indices.

Following an equally-weighted allocation is equivalent to holding an equal dollar allocation, which does not necessarily lead to an equal risk allocation. Formally, the risk contribution of a stock to the total risk of a portfolio is given by the weight of the stock in the portfolio times the marginal contribution

of the stock to total portfolio volatility. Qian (2006) shows that decomposing total portfolio volatility in terms of its constituents' risk contributions is also related to the expected contributions to the portfolio losses, particularly when considering extreme losses. In what follows, we consider two approaches to managing portfolio risk: one approach based on minimising portfolio volatility (global minimum variance or GMV approach) and another approach based on imposing equal contribution of all constituents to portfolio volatility (heuristic equal risk contribution or ERC approach).

Absolute risk management without factor risk exposure constraints

In our attempt to design an efficient allocation to smart factor indices, we first impose that all constituents in the portfolio have the same contribution to portfolio risk (ERC). If one makes the explicit assumption that all pairwise correlation coefficients across constituents are identical, then the equal risk constribution weights can be obtained analytically and are proportional to the inverse volatility of the smart factor indices. In the general case, i.e. without the assumption of identical pairwise correlations across stocks, the risk parity methodology does not yield a closed-form solution. However, Maillard, Roncalli and Teïletche (2010) propose numerical algorithms to compute risk parity portfolios.

Overall, ERC and EW are two competing ways of implementing agnostic diversification. When looking at the empirical analysis performed in the global developed universe shown in Exhibit 1 below, we find that the allocation between the equally-weighted and the ERC schemes can exhibit strong differences. For example, the largest average weight over the period under study is given to the Japan Low Volatility

smart factor index (7.45%), whereas the lowest weight is given to the Dev. Europe ex UK Value smart factor index (3.78%). We also find that the equal risk contribution can lead to regional allocations that strongly deviate from the corresponding allocation within a capweighted index, where the larger markets (e.g., the US) strongly dominate smaller markets, such as Japan for example.

We have also implemented an allocation between smart factor indices based on minimising the risk of the allocation, expressed by its volatility (GMV). In this case the GMV portfolio of the 20 index constituents, which is the efficient portfolio that requires only covariance matrix input, the sample covariance matrix is estimated using the past eighteen months of weekly data as an input. Long-only constraints are applied

to the standard minimum volatility problem, i.e. minimise portfolio volatility as given by this expression:

 $\min_{(w_i)_{i=1,\dots,N}} v(w) = w'Cw$

To avoid introducing excessively strong biases with respect to the CW index, and even though the focus is not on relative risk management in this illustration, we also introduce a set of constraints dedicated to ensuring that each sub-region is not too strongly under- or over-represented with respect to its market capitalisation in the CW global developed index, i.e. we define the weight to lie between half the region's market cap weight and twice its market cap weight.

Exhibit 2 shows that the GMV

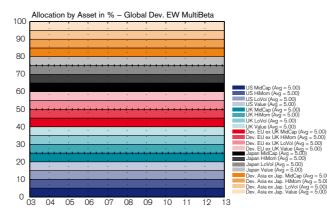
allocation with geographical constraints leads to a portfolio that is almost exclusively invested in the lowest volatility smart index for each subregion: (on average, 52.47% low volatility smart factor US index, 8.60% low volatility smart factor UK index, 16.42% low volatility smart factor Dev. Europe ex UK index, 12.68% low volatility smart factor Japan index, and 6.74% low volatility smart factor Asia Pacific ex Japan index). In the end, this process leads to a dynamically managed portfolio of the 20 constituents that should achieve low volatility but that is highly concentrated.

Exhibit 2 also shows that the portfolio variance is almost exclusively driven by the low volatility factor, an observation that stresses the need for the introduction of risk factor budgeting

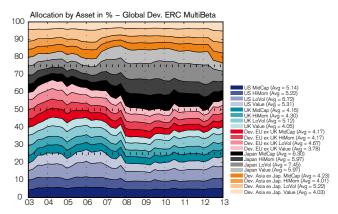
Exhibit 1: EW and ERC Allocations to Smart Factor Diversified Multi-Strategy Indices and Risk Contributions (Developed Universe)

The graph compares the allocation and risk contributions of Diversified Multi-Strategy indices: the equal combination of the twenty Diversified Multi-Strategy indices converted into US Dollars with stock selection based on mid cap, momentum, low volatility, and value in the five sub-regions US, UK, Dev. Europe ex UK, Japan and Asia Pacific ex Japan, and the ERC combination of the same twenty constituents. The period is from 31-December-2003 to 31-December-2013.

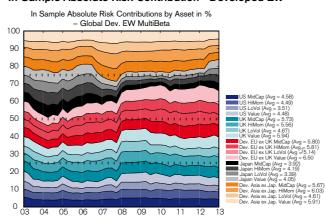
Weight Distribution - Developed EW



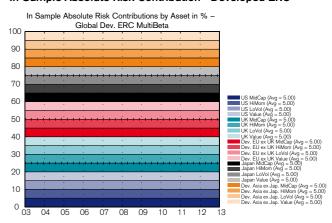
Weight Distribution - Developed ERC



In-Sample Absolute Risk Contribution - Developed EW



In-Sample Absolute Risk Contribution - Developed ERC



constraints in order to better balance the factor contributions to the risk of the portfolio. ³

Introducing risk budgeting constraints

Having an equal contribution from the constituents to the overall portfolio risk is not identical to having an equal contribution from the factors. It is only if both the factors and the factor indices are perfectly "pure," that is uncorrelated, that these two approaches coincide, which is not the case with smart factor indices. However, often it is the objective of investors to have an equal contribution to the underlying risk factors because risk contributions are perceived as indicators of the factor's expected contribution to future losses (see Qian (2006)). In this way, integration of factor risk constraints in the allocation process takes into account the imperfections of existing single (smart) factor indices.

In the following, we use the factor exposure of the smart factor indices to analyse the question. We will compute exposure with respect to the equally-weighted version of the factors, since they are the most neutral reference portfolios. As a neutral target, we may seek to impose an equal contribution

of the factors to the variance coming from the factors. This extension of the equal risk contribution (ERC) approach from the constituents to the factors leads to linear constraints in the design of the portfolio. This method of ERC of factors (along with EW of factors) is a reasonable approach for investors who are agnostic about the future performance of any single factor and therefore don't want to take a bet on one factor over another. In practice, in the absence of any active views on factors, these approaches are quite robust allocation techniques.

We introduce factor risk budgeting constraints to the portfolio allocation process so as to avoid the domination of any one particular factor (such as the domination of the low volatility factor). When the number of constituents N is greater than the number of factor constraints K, and long-short solutions are allowed, an infinite number of portfolios satisfy a given set of factor risk budgets (e.g., factor risk parity exposure). In a long-only context, we may have zero or multiple solutions. When no solution exists, one can start with the long-short version and rescale the weights to avoid short positions.

When multiple solutions exist, one can address the diversification of specific

risks, e.g., from a scientific perspective, by minimising portfolio variance subject to factor risk parity constraints. We may also maximise portfolio deconcentration, measured by the effective number of constituents, again subject to factor risk parity constraints: ⁴

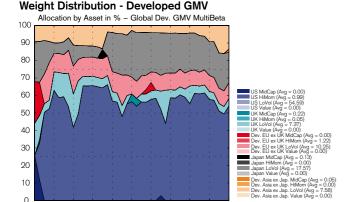
Exhibit 3 shows max-deconcentration and GMV allocations under risk parity as well as geographical constraints.

First of all, we notice that factor risk parity is satisfied, and that the portfolio is no longer simply invested in the lowvolatility constituents. Similarly to the allocation we obtained in the previous case, we also notice that the aggregated weights in the different sub-regions appear to represent the sub-region market capitalisations more fairly due to the presence of regional constraints. We also note that the max-deconcentration approach shows a more stable allocation over time compared to the GMV, which is still sensitive to changes in input parameters. Also we see that the addition of factor risk parity constraints forces the allocations to spread the country weight more evenly among the different tilts.

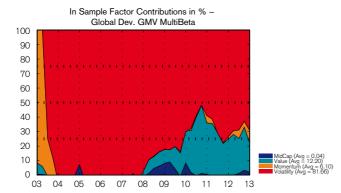
Exhibit 4 reports the risk and returns characteristics of various multi-smart-beta allocation portfolios, and compares the results. We note that the GMV allocation process leads to the lowest

Exhibit 2: GMV Allocations to Smart Factor Diversified Multi-Strategy Indices under Geographical Constraints and Risk Contributions (Developed Universe)

The graph shows the allocation and risk contributions of the GMV allocation invested in the twenty Diversified Multi-Strategy indices converted into US Dollars with stock selection based on mid cap, momentum, low volatility, and value in the five US, UK, Dev. Europe ex UK, Japan and Asia Pacific ex Japan sub-regions. Both risk parity and geographical constraints are imposed on the resulting portfolios. The period is from 31-December-2003 to 31-December-2013.



In-Sample Factor Contribution - Developed GMV

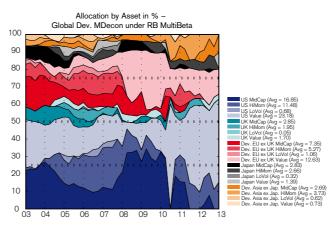


- ³ The contribution of the low volatility factor is sometimes even greater than 100%, while other factors have a negative contribution to portfolio variance due to the presence of non-zero correlations between the smart factor indices and also between the long-short factors. For example, increasing the exposure to a factor that is negatively correlated with other factors may contribute to decreasing the portfolio variance.
- ⁴ Of course, in the absence of constraints, maximising deconcentration simply leads to giving a weight of 1/N to each constituent in the universe.

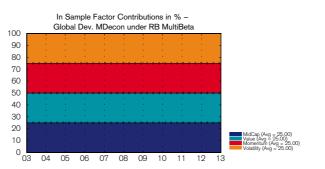
Exhibit 3: Max Deconcentration and GMV Allocations under Risk Factor and Geographical Constraints (Developed Universe).

The graph shows the allocations and factor contributions of the max-deconcentration and GMV Diversified Multi-Strategy indices invested in the twenty Diversified Multi-Strategy indices with stock selection based on mid cap, momentum, low volatility, and value in the five US, UK, Dev. Europe ex UK, Japan and Asia Pacific ex Japan sub-regions. Both risk parity and geographical constraints are imposed onto the resulting portfolios. The period is from 31-December-2003 to 31-December-2013.

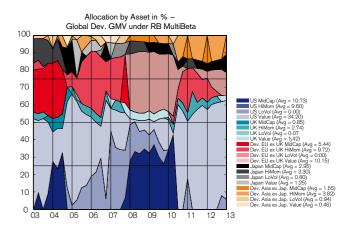
Weight Distribution – Max Deconcentration with factor risk constraints



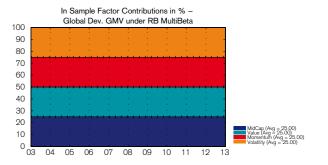
In-Sample Factor Contribution - Max
Deconcentration with factor risk constraints



Weight Distribution - GMV with factor risk constraints



In-Sample Factor Contribution - GMV with factor risk constraints



volatility. Also, we notice that the EW and ERC allocations have higher returns and higher volatilities than the GMV, as is often the case. We note further that the introduction of factor risk parity constraints has led to a substantial improvement in information ratios with an information ratio above 1 for the max-deconcentration allocation under geographical and risk parity constraints. This shows that the introduction of factor risk parity constraints leads to a stabilisation of the portfolio that has resulted in strong outperformance (3.37%) over the CW index, with a tracking error barely greater than 5%. The introduction of factor risk parity constraints leads to 100% outperformance probabilities over a 3-year horizon.

In Exhibit 5, we analyse the performances in bull versus bear

100%
outperformance
probabilities
over a 3-year
borizon

market regimes (defined as positive versus negative returns for the CW index). We observe that the addition of risk parity constraints to the GMV allocation tends to stabilise the returns across market conditions. For example, in the absence of factor risk parity

constraints, the GMV allocation leads to a massive outperformance of 11.94% with respect to the CW index in bear markets, which is due to the almost exclusive domination of the low volatility factor, with a defensive bias that proves extremely useful in such market conditions. On the other hand, the relative return in bull market is negative at -3.90% due to the performance drag associated with exclusively holding defensive equity exposure in bull market conditions. In this context, one key advantage of the introduction of factor risk parity constraints is that it leads to a much more balanced return profile across market conditions with positive outperformance in both bear and bull markets (at 2.66% and 3.18% respectively).

We have shown that simple allocations that do not balance their exposures to

Exhibit 4: Multi-Beta Allocations across Smart Factor Indices (Developed Universe)

The table compares performance of the EW, ERC, and GMV and both the max-deconcentration and GMV Diversified Multi-Strategy indices under geographical and risk parity constraints, invested in the twenty Diversified Multi-Strategy indices with stock selection based on mid cap, momentum, low volatility, and value in the five US, UK, Dev. Europe ex UK, Japan and Asia Pacific ex Japan sub-regions. The period is from 31-December-2003 to 31-December-2013 (10 years). Outperformance Probability is the probability of obtaining positive excess returns over CW if one invests in the strategy at any point in time for a period of 3 years. It is computed as the frequency of positive values in the series of excess returns assessed over a rolling window of 3 years and step size of one week covering the entire investment horizon.

| | | Diversified Multi-Strategy | | | | | | |
|-----------------------|--------------------|--------------------------------|---------------------------------|---------------------------------|--|--------------------------------------|--|--|
| Developed (2004-2013) | CW (All Stocks) | Multi Beta EW Allocation | Multi Beta ERC Allocation | Multi Beta GMV Allocation | Multi-Beta Max Deconc. Fact Allocation | Multi Beta GMV-Fact Allocation | | |
| Ann Returns | 7.80% | 11.37% | 11.07% | 10.57% | 11.17% | 10.88% | | |
| Ann Volatility | 17.09% | 15.32% | 14.33% | 12.84% | 17.23% | 17.21% | | |
| Sharpe Ratio | 0.36 | 0.64 | 0.66 | 0.70 | 0.56 | 0.54 | | |
| Max Drawdown | 57.13% | 54.40% | 51.82% | 45.07% | 55.22% | 55.32% | | |
| Excess Returns | - | 3.56% | 3.27% | 2.76% | 3.37% | 3.07% | | |
| Tracking Error | - | 6.75% | 7.51% | 6.36% | 3.08% | 3.34% | | |
| 95% Tracking Error | - | 13.84% | 14.89% | 11.85% | 5.19% | 5.55% | | |
| Information Ratio | - | 0.53 | 0.44 | 0.43 | 1.09 | 0.92 | | |
| Outperf. Prob. (3Y) | - | 98.36% | 89.34% | 89.07% | 100.00% | 100.00% | | |
| Max Rel. Drawdown | - | 6.35% | 9.54% | 13.10% | 4.03% | 5.47% | | |

Exhibit 5: Multi-Beta Allocations across Smart Factor Indices in Bull/Bear Regimes (Developed Universe)

The table compares conditional performance of the EW, ERC, and GMV and both the max-deconcentration and GMV Diversified Multi-Strategy indices under geographical and risk parity constraints, invested in the twenty Diversified Multi-Strategy indices with stock selection based on mid cap, momentum, low volatility, and value in the five US, UK, Dev. Europe ex UK, Japan and Pacific Asia ex Japan sub-regions. The period is from 31-December-2003 to 31-December-2013 (10 years). The quarters with positive market returns are considered bullish and the quarters with negative returns are considered bearish.

| | Diversified Multi-Strategy | | | | | | | | |
|-----------------------|--------------------------------|---------------------------------|---------------------------------|--|-----------------------------------|--|--|--|--|
| Developed (2004-2013) | Multi Beta EW Allocation | Multi Beta ERC Allocation | Multi Beta GMV Allocation | Multi-Beta Max Deconc. Fact Allocation | Multi Beta GMV-Fact Allocation | | | | |
| Ann. Ret. Bull | 31.58% | 29.55% | 25.18% | 32.89% | 32.26% | | | | |
| Ann. Vol. Bull | 11.71% | 11.09% | 9.42% | 12.85% | 12.85% | | | | |
| Ann. Rel. Ret. Bull | 2.50% | 0.48% | -3.90% | 3.81% | 3.18% | | | | |
| Tracking Error Bull | 5.03% | 5.94% | 5.06% | 2.53% | 2.74% | | | | |
| Ann. Ret. Bear | -24.51% | -22.42% | -17.23% | -26.67% | -26.50% | | | | |
| Ann. Vol. Bear | 21.33% | 19.79% | 18.40% | 24.42% | 24.38% | | | | |
| Ann. Rel. Ret. Bear | 4.65% | 6.74% | 11.94% | 2.50% | 2.66% | | | | |
| Tracking Error Bear | 9.64% | 10,27% | 8.62% | 4.08% | 4.43% | | | | |

the factors may be too exposed to the low-volatility factor, which may lead to lower relative returns with respect to the cap-weighted index, particularly in bull market regimes.

Long-term evidence in the USA universe

The limited availability of data in the global stock universe caused us to restrict the analysis to a 10-year period. In order to test the robustness of the allocation schemes, we replicate the allocations in the US stock universe

for which data is available for 40 years. This period consists of varying degrees of market environments and therefore allows us to look at the performance of different allocations over time through a conditional analysis tool.

The first observation from Exhibit 6 is that the results for the USA are similar in nature to those for Developed. All allocations outperform the CW benchmark by a large margin (>3.8%). As expected, the information ratio of factor-risk-parity-constrained Max Deconcentration is 0.81, as

compared to 0.76 for EW allocation, showing that the constraints fulfil their long-term objective. Exhibit 7 shows that all allocations are quite stable across different market conditions. They are able to outperform the CW benchmark in both bull and bear market conditions.

Adding value through allocation choices

We find that value can be added at the allocation stage, where the investor can control for the dollar and risk

Exhibit 6: Multi-Beta Allocations across Smart Factor Indices (US Universe)

The table compares the performance of the EW, ERC and max-deconcentration indices with risk parity constraints, invested in the four Diversified Multi-Strategy indices with stock selection based on mid cap, momentum, low volatility, and value in the US. The period is from 31-December-1972 to 31-December-2012 (40 years). Outperformance Probability is the probability of obtaining positive excess returns over CW if one invests in the strategy at any point in time for a period of 3 years. It is computed as the frequency of positive values in the series of excess returns assessed over a rolling window of 3 years and step size of one week covering the entire investment horizon.

| USA Long Term | CW | Diversified Multi-Strategy | | | | | |
|---------------------|--------------|-----------------------------|------------------------------|---|--|--|--|
| (1973-2012) | (All Stocks) | Multi Beta EW Allocation | Multi Beta ERC Allocation | Multi-Beta Max Deconc. Fact Allocation | | | |
| Ann Returns | 9.74% | 13.72% | 13.63% | 14.01% | | | |
| Ann Volatility | 17.47% | 15.75% | 15.67% | 16.41% | | | |
| Sharpe Ratio | 0.24 | 0.52 | 0.52 | 0.52 | | | |
| Max Drawdown | 54.53% | 53.86% | 53.62% | 56.56% | | | |
| Excess Returns | - | 3.98% | 3.89% | 4.27% | | | |
| Tracking Error | - | 5.23% | 5.25% | 5.27% | | | |
| 95% Tracking Error | - | 8.95% | 9.10% | 8.69% | | | |
| Information Ratio | - | 0.76 | 0.74 | 0.81 | | | |
| Outperf. Prob. (3Y) | - | 80.38% | 80.43% | 78.83% | | | |
| Max Rel. Drawdown | - | 33.65% | 43.46% | 33.87% | | | |

Exhibit 7: Multi-Beta Allocations across Smart Factor Indices in Bull/Bear Regimes (Developed and USA Universe)

The table compares performance of the EW, ERC and max-deconcentration indices with risk parity constraints, invested in the four Diversified Multi-Strategy indices with stock selection based on mid cap, momentum, low volatility, and value in the US. The period is from 31-December-1972 to 31-December-2012 (40 years). The quarters with positive market returns are considered bullish and the quarters with negative returns are considered bearish.

| USA Long Term | Diversified Multi-Strategy | | | | | | | |
|---------------------|-----------------------------|------------------------------|---|--|--|--|--|--|
| (1973-2012) | Multi Beta EW Allocation | Multi Beta ERC Allocation | Multi-Beta Max Deconc. Fact Allocation | | | | | |
| Ann. Ret. Bull | 34.83% | 34.57% | 36.14% | | | | | |
| Ann. Vol. Bull | 12.94% | 12.85% | 13.42% | | | | | |
| Ann. Rel. Ret. Bull | 3.03% | 2.76% | 4.34% | | | | | |
| Tracking Error Bull | 4.45% | 4.46% | 4.54% | | | | | |
| Ann. Ret. Bear | -20.17% | -20.04% | -21.13% | | | | | |
| Ann. Vol. Bear | 20.23% | 20.14% | 21.14% | | | | | |
| Ann. Rel. Ret. Bear | 4.83% | 4.96% | 3.87% | | | | | |
| Tracking Error Bear | 6.57% | 6.58% | 6.53% | | | | | |

contributions of various constituents or factors to the absolute risk (volatility) of the portfolio. As a result, extremely substantial levels of risk-adjusted outperformance (information ratios) can be achieved even in the absence of views on factor returns. The portfolio strategies we have presented in this brief article can be regarded as robust attempts at generating an efficient strategic factor allocation process in the equity space. One of the important conclusions of our research is to show that it is possible to satisfy factor risk parity objectives in a long-only world by using long-only smart factor indices that by construction cannot be orthogonal to

each other, but, while lacking "purity," are well diversified. Other approaches which would extend the present illustrations could explicitly focus on the management of relative risk. Moreover, active portfolio managers may generate additional value by incorporating forecasts of factors returns at various points of the business cycle in the context of tactical factor allocation decisions.

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References

- Maillard S., T. Roncalli and J. Teïletche. 2010. The Properties of Equally Weighted Risk Contributions Portfolios. *Journal of Portfolio Management* 36(4): 60-70.
- Qian, E. 2006. On the Financial Interpretation of Risk Contribution: Risk Budgets Do Add Up. *Journal of Investment Management* 4(4).





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A Relative Risk Perspective on Risk Allocation with Smart **Factor Indices**

By Noël Amenc, Romain Deguest and Ashish Lodh

any investors are seeking to improve the performance of their equity portfolios by capturing exposure to rewarded factors. Investors may thus explore a variety of portfolio strategies which can be regarded as robust attempts at generating an efficient strategic factor allocation process in the equity space for different sets of objectives and constraints. Allocation can be done in the most simple manner, such as equal dollar contribution/equal weighting (EW), or equal risk contribution (ERC), or in a more sophisticated manner of diversification, such as volatility minimisation (GMV). For the objectives involving risk parameters, allocation methods can broadly be categorised into two groups depending on the risk dimension they deal with - absolute risk and relative risk. In this article, we focus on allocation across smart factor indices from *relative risk* perspective.

It is often the case that investors maintain the cap-weighted index as a benchmark, which has the merit of macro-consistency and is wellunderstood by all stakeholders. In this context, a multi-smart-beta solution can be regarded as a reliable cost-efficient substitute for expensive active managers, and the most relevant perspective is not an absolute return perspective but a relative perspective with respect to the cap-weighted index. In what follows, we focus on two approaches:

- *Naive diversification*: a relative equal risk allocation (R-ERC) portfolio, which focuses on equalising the contribution of the smart factor-tilted indices to the portfolio tracking error.
- Scientific diversification: a relative global minimum variance portfolio

(R-GMV), also known as minimum tracking error portfolio, which focuses on minimising the variance of the portfolio relative returns with respect to the cap-weighted index.

It should be noted that controlling for factor exposure biases from an absolute risk budgeting perspective is useful, but this is no longer a key required ingredient since the CW index already provides a proper anchor point that is an implicit, as opposed to explicit, reference set of factor exposures. In the same manner, we find that regional constraints are no longer needed, since a portfolio seeking to equalise the contributions of the 20 constituents to the portfolio tracking error, or seeks to minimise the tracking error, will not lead to a severe overweighting of smaller regions with respect to larger regions, in contrast to what has been found from an absolute risk perspective.

Methodology

Relative ERC is implemented in a way similar to ERC allocation, the only difference being that tracking error contributions are equalised instead of volatility contributions. If we define the contribution of component *i* to portfolio tracking error as:

$$C_i^{trk}(w) = \frac{1}{2} \frac{\partial TE^2}{\partial w}$$
, $w_i \text{ with } \sum_{i=1}^N C_i^{trk}(w) = TE^2$

The relative ERC portfolio is defined as the allocation w that satisfies the following identity:

$$\frac{C_i^{trk}(w)}{TE^2} = \frac{1}{N} \text{ for all } i$$

The relative GMV approach follows a mean variance optimisation to minimise total portfolio tracking error under

long-only constraints. Mathematically it can be written as (Σ is the covariance of excess returns over the CW benchmark):

Min
$$(w^T. \Sigma.w)$$
 subject to $1^T.w$
= 1 and $w_i \ge 0$ for all i

We discuss the composition and performance statistics of Developed and US portfolios. The Developed dataset extends over the 10-year period from 31-December-2003 to 31-December-2013 and uses 5 subregions of the global developed universe: US, UK, Dev Europe ex UK, Japan and Asia Pacific ex Japan. Using four smart multi-strategy indices as proxies for the value, size, momentum, and volatilityrewarded tilts in each sub-region; we obtain a total of 5x4 = 20 constituents.

Risk contributions and performance

In Exhibit 1, we show the allocations of the relative GMV and relative ERC portfolios. First of all, we find again that the relative ERC allocation is more stable over time, which is due to the higher sensitivity of the relative GMV allocation to the parameter estimates, confirming a higher degree of robustness with the ERC approach. Even though both allocation strategies rely on risk parameter estimates, scientific diversification tends to over-use input information compared to the more agnostic risk budgeting diversification, which makes a more parsimonious use of input estimates (see Roncalli (2013) for more details and interpretations for the higher robustness of ERC portfolios with respect to errors in risk parameter estimates).

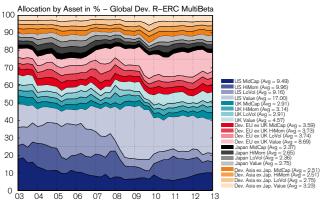
Secondly, by construction, we observe that the relative ERC leads to identical

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Exhibit 1 – Relative GMV and Relative ERC Allocations to Smart Factor Indices and Risk Contributions (Developed Universe):

The graph compares the allocation and risk contributions of Diversified Multi-Strategy indices: the relative GMV and relative ERC allocations invested in the four Diversified Multi-Strategy indices with stock selection based on mid cap, momentum, low volatility, and value. The period is from 31-December-2003 to 31-December-2013.

Weight Distribution - Relative ERC (Developed)



In-Sample Relative Risk Contribution by asset – Relative ERC (Developed)

error. However, the relative GMV

portfolio involves non-equal time-

varying contributions from various

portfolio. This observation is in line

with the relative GMV objective, i.e.

that have lower tracking error.

constituents to the tracking error of the

the components that have large tracking

error are under-weighted relative to ones

Exhibit 3 displays the risk and return

GMV allocation strategies. We note that

the focus on relative return leads to low

tracking error levels. For example, the

ex-post tracking error is around 2.50%

for these portfolios. Relative GMV, as

per its objective, results in lower tracking

error (2.43%) compared to relative ERC

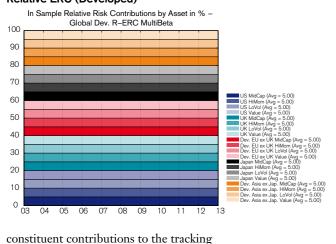
(2.56%). However, relative ERC exhibits

Such low tracking error levels, associated

greater outperformance (+3.12%) compared to relative GMV (+2.15%).

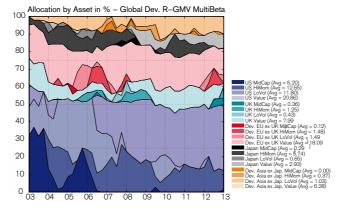
with substantial outperformance, eventually leads to exceedingly high

characteristics of the relative ERC and

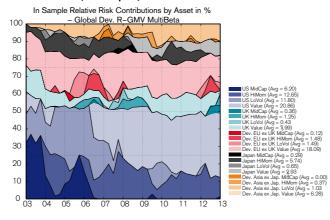


The benefit
of exposure to
multiple factors
can be seen from
conditional
performance
analysis.'

Weight Distribution - Relative GMV (Developed)



In-Sample Relative Risk Contribution by asset – Relative GMV (Developed)



information ratios. In particular, the relative ERC has an information ratio of 1.22, which is the highest level among all portfolio strategies tested so far, with an outperformance probability of 100% over any given three-year investment horizon during the same period. We also find that the focus on relative risk leads to lower tracking errors in bull and bear market regimes compared to their absolute risk counterparts.

The benefit of exposure to multiple factors can be seen from conditional

The benefit of exposure to multiple factors can be seen from conditional performance analysis. Both allocations are able to outperform the CW benchmark in both bull and bear market conditions. For example, relative allocation beats the CW benchmark by 2.30% in bull markets and by 3.92% in bear markets.

Relative risk allocation using long term USA factor indices

Since Developed track records are limited to a 10-year time period, we

Exhibit 2– Relative ERC and Relative GMV Allocation to the CW Index across Smart Factor Indices (Developed Universe):

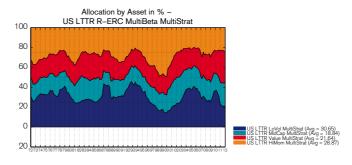
The table compares the performance and risk of Scientific Beta Diversified Multi-Strategy indices converted into US dollars. We look at relative ERC and relative GMV allocations invested in the twenty Diversified Multi-Strategy indices with stock selection based on mid cap, momentum, low volatility, and value in the five US, UK, Dev. Europe ex UK, Japan and Asia Pacific ex Japan sub-regions. Outperformance Probability is the probability of obtaining positive excess returns over CW if one invests in the strategy at any point in time for a period of 3 years. It is computed as the frequency of positive values in the series of excess returns assessed over a rolling window of 3 years and step size of one week covering the entire investment horizon. The quarters with positive market returns are considered bullish and the quarters with negative returns are considered bearish. The period is from 31-December-2003 to 31-December-2013.

| | | Diversified M | lulti-Strategy | | Diversified N | Multi-Strategy |
|-----------------------|--------------------|--|-----------------------------------|---------------------|--|--|
| Developed (2004-2013) | CW (All Stocks) | Multi-Beta Relative ERC Allocation | tive ERC Relative GMV (2004-2013) | | Multi-Beta Relative ERC Allocation | Multi-Beta Relative GMV Allocation |
| Annual Returns | 7.80% | 10.92% | 9.96% | Ann. Ret. Bull | 31.38% | 31.02% |
| Annual Volatility | 17.09% | 16.10% | 16.64% | Ann. Vol. Bull | 11.95% | 12.25% |
| Sharpe Ratio | 0.36 | 0.58 | 0.50 | Ann. Rel. Ret. Bull | 2.30% | 1.95% |
| Max Drawdown | 57.13% | 54.14% | 55.50% | Tracking Error Bull | 2.09% | 2.01% |
| Excess Returns | - | 3.12% | 2.15% | Ann. Ret. Bear | -25.25% | -26.93% |
| Tracking Error | - | 2.56% | 2.43% | Ann. Vol. Bear | 22.88% | 23.75% |
| 95% Tracking Error | - | 4.70% | 4.27% | Ann. Rel. Ret. Bear | 3.92% | 2.23% |
| Information Ratio | - | 1.22 | 0.88 | Tracking Error Bear | 3.41% | 3.21% |
| Outperf. Prob. (3Y) | - | 100.00% | 89.34% | | | |
| Max Rel. Drawdown | - | 5.10% | 4.95% | | | |

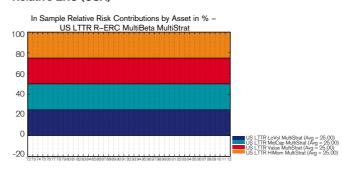
Exhibit 3 - Relative GMV and Relative ERC Allocations to Smart Factor Indices and Risk Contributions (US Universe):

The graph compares the allocation and risk contributions of Diversified Multi-Strategy indices: the relative GMV and ERC allocations invested in the four Diversified Multi-Strategy indices with stock selection based on mid cap, momentum, low volatility, and value, and the ERC combination of the same four constituents. The Relative GMV strategy has been derived with the following additional weight constraints: $1/\delta^*N < w < \delta/N$, where N=4 constituents and δ =2. The period is from 31-December-1972 to 31-December-2012.

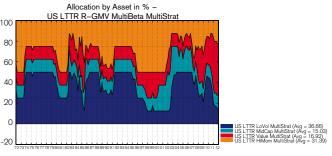
Weight Distribution - Relative ERC (USA)



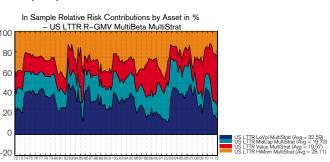
In-Sample Relative Risk Contribution by asset – Relative ERC (USA)



Weight Distribution - Relative GMV (USA)



In-Sample Relative Risk Contribution by asset – Relative GMV (USA)



Article 3

Exhibit 4 – Relative ERC and Relative GMV Allocation to the CW Index across Smart Factor Indices (US Universe):

The table compares the performance and risk of the Scientific Beta Diversified Multi-Strategy indices. We look at relative ERC and relative GMV allocations in the four Diversified Multi-Strategy indices with stock selection based on mid cap, momentum, low volatility, and value respectively. All statistics are annualised and daily total returns from 31-December-1972 to 31-December-2012 are used for the analysis. The S&P 500 index is used as the cap-weighted benchmark. Yield on Secondary US Treasury Bills (3M) is used as a proxy for the risk-free rate. Outperformance Probability is the probability of obtaining positive excess returns over CW if one invests in the strategy at any point in time for a period of 3 years. It is computed as the frequency of positive values in the series of excess returns assessed over a rolling window of 3 years and step size of one week covering the entire investment horizon. The quarters with positive market returns are considered bullish and the quarters with negative returns are considered bearish.

| | | Diversified M | lulti-Strategy | | Diversified Multi-Strategy | | |
|-----------------------------|--------------------|--|--|-----------------------------|--|--|--|
| US Long Term (1973-2012) | CW (All Stocks) | Multi-Beta Relative ERC Allocation | Multi-Beta Relative GMV Allocation | US Long Term (1973-2012) | Multi-Beta Relative ERC Allocation | Multi-Beta Relative GMV Allocation | |
| Annual Returns | 9.74% | 13.53% | 13.45% | Ann. Ret. Bull | 34.72% | 34.39% | |
| Annual Volatility | 17.47% | 15.69% | 15.60% | Ann. Vol. Bull | 12.89% | 12.97% | |
| Sharpe Ratio | 0.24 | 0.51 | 0.51 | Ann. Rel. Ret. Bull | 2.92% | 2.59% | |
| Max Drawdown | 54.53% | 53.30% | 52.64% | Tracking Error Bull | 4.20 % | 3.78% | |
| Excess Returns | - | 3.79% | 3.71% | Ann. Ret. Bear | -20.44% | -21.02% | |
| Tracking Error | - | 4.91% | 4.79% | Ann. Vol. Bear | 20.14% | 20.15% | |
| 95% Tracking Error | - | 8.11% | 7.99% | Ann. Rel. Ret. Bear | 4.56% | 3.97% | |
| Information Ratio | - | 0.77 | 0.77 | Tracking Error Bear | 6.12% | 5.49% | |
| Outperf. Prob. (3Y) | - | 80.90% | 81.31% | | | | |
| Max Rel. Drawdown | - | 28.74% | 27.00% | | | | |

use the US stock universe (of the 500 largest market-cap stocks) to redo the relative risk allocation exercise to ensure the robustness of our results. The US universe gives us the advantage of a much longer history (40 years) but also limits us to using 4 smart factor indices (instead of 20 indices in the international domain). For the following illustrations, long-term (40vear) data from 31-December-1973 to 31-December-2013 is used for the four smart multi-strategy indices - Mid Cap. Momentum, Low Volatility and Value. All other construction principles remain the same as before.

Exhibit 3 shows that over long periods, the weight distribution in the ERC allocation remains quite stable. The GMV allocation is relative time varying, over-weighting the factor that is responsible for the lowest tracking error each time.

When analysing the risk and performance indicators in Exhibit 4, we observe that the relative GMV, which is supposed to minimise the tracking error, achieves a tracking error of 4.79% compared to relative ERC, with a tracking error of 4.91%. As observed in the case of the Developed universe, both allocations result in high outperformance, with relative ERC slightly better (at +3.79%) than relative GMV (+3.71%). The conditional performance over the long term constitutes many market cycles, including the technology bubble and the financial crisis. The fact that both allocations outperform the benchmark in varying market conditions reconfirms the robustness of these strategies.

We find that value can be added through relative ERC and relative GMV at the allocation stage, for investors with a tracking error budget. As a result,

Extremely substantial levels of risk-adjusted outperformance (information ratios) can be achieved even in the absence of views on factor returns

extremely substantial levels of riskadjusted outperformance (information ratios) can be achieved even in the absence of views on factor returns. The portfolio strategies we have presented in this article can be regarded as robust attempts at generating an efficient strategic factor allocation process in the equity space in the context of benchmarked investment management. While possibilities for adding value through smart beta allocation are manifold, the robust performance improvements obtained through relative ERC and relative GMV allocations to the four main consensual factors displayed above in this article, provide evidence that the benefits of multi-factor allocations exist in a context of strong relative risk constraints and are sizable.

By Noël Amenc, Professor of Finance, EDHEC Business School, Director, EDHEC-Risk Institute, CEO, ERI Scientific Beta; Romain Deguest, Senior Research Engineer, EDHEC-Risk Institute; Ashish Lodh, Senior Quantitative Analyst, ERI Scientific

References

 Roncalli, T. 2013. Introduction to Risk Parity and Budgeting. Chapman & Hall. CRC Financial Mathematics Series.

How Investable are Smart Beta Indices?

By Noël Amenc, Felix Goltz and Nicolas Gonzalez

Tith the advent of smart beta equity indices, which represent alternatives to marketcap weighted indices, a major question has been raised on their investability: at what cost will investors be able to trade the index constituents in the same proportions as the underlying strategy? In fact, departing from the traditional cap-weighting investment scheme leads to risks that are sizable and significantly different, as shown in Amenc, Goltz and Lodh (2012) and Amenc, Goltz and Martellini (2013). These include common exposures to systematic risk factors such as size and liquidity.

Also, in contrast to cap-weighted indices, which are deemed to be buyand-hold investments, and which are only marginally reviewed for the (often quarterly) addition and deletion of constituents as well as regular corporate events, smart beta indices exhibit higher levels of turnover than their cap-weighted counterparts (see e.g. Amenc et al. (2011)). Importantly, for any level of liquidity, the level of turnover in the index will impact the performance of the tracking fund through the frequency of occurrence of transaction costs.

Clearly, investing in smart beta indices requires investors to have access to solutions where implementation costs and liquidity risks are thoroughly considered. A key implication is that the smart beta index turnover and capacity constraints need to be methodologically and carefully handled through the construction of the index. The objective of this article is to describe how to ensure the investability of the indices by managing turnover control and capacity constraints. The ERI Scientific Beta methodology has been used to exemplify best practices in this area.

Consistent framework

ERI Scientific Beta indices are derived from a consistent index design framework referred to as Smart Beta 2.0. An investor can select an index by making conscious and explicit choices of risks along the different dimensions of this framework. The objective of such a consistent framework is to avoid unintended risks due to ill-defined consequences of ad hoc methodologies.

Thanks to the consistent design framework, clear rules concerning liquidity and turnover can be aimed at facilitating implementation of the indices. Adjustments are performed through the main steps in the index construction process, which aim to ensure the investability of the indices, either by reducing implementation costs, or by allowing their liquidity profile to be improved.

Clear rules
concerning liquidity
and turnover can be
aimed at facilitating
implementation
of the indices.'

Turnover control

The turnover of an equity index is an early indication of the aggregated trading activity of funds that will track that index. Although knowledge of a portfolio's turnover does not provide a precise measure for estimating the actual costs of trading, it provides an intuitive and parsimonious idea of the fund's trading activity and, as such, is a sensible indicator.

Turnover varies greatly from one index to another, and the methods for managing it are a complex problem in constructing indices. ERI Scientific Beta has opted for a conditional (or trigger) rebalancing approach described in Martellini and Priaulet (2002) and Leland (1999). The trigger approach activates rebalancing whenever the gap between the current index weights and new target weights reaches a specific threshold (e.g. ±5% or ±10%). The main advantage of the trigger approach is that it avoids unnecessary rebalancing unless a significant amount of new information has been received since the last index rebalancing, hence avoiding rebalancing due to noise.

The threshold level of an index is determined through a calibration procedure over its back-test history. First, different versions of the index are constructed over the calibration period, each with a conditional rebalancing dictated by a threshold spanning 0% to 100%. Then, the smallest threshold that results in an average one-way annual turnover below or equal to 30% over the calibration period is used as the specific turnover threshold for that index in its live period.5 Finally, irrespective of whether or not the threshold mentioned above is reached, suggested optimised weights will be used if the index has not been rebalanced optimally for seven consecutive quarters.

As shown in Exhibit 1, before turnover control, Scientific Beta USA Indices exhibit levels of turnover that can exceed reasonable investability levels. This is notably the case for the Maximum Decorrelation, Efficient Minimum Volatility and Efficient Maximum Sharpe ratio Indices, which respectively exhibit 59.51%, 54.81% and 65.02% average annualised one-way turnover over the period from 29/06/1970 to 21/12/2012. After controlling for turnover, the same indices exhibit a much more reasonable level of turnover (respectively 29.22%, 29.83% and 27.84%).

⁵ Index specific turnover thresholds may be re-calibrated at some point in time in order to reflect structural changes in market conditions

Exhibit 1: Comparison of performance, turnover and liquidity before and after turnover control.

The first panel reports the statistics for the indices before any turnover control is applied, whereas the second panel reports the statistics for the indices after turnover control is applied. The annualised 1-way turnover and average float is calculated at the end of each quarter and are averaged over the analysis period. The net returns of transaction costs are obtained using two levels of transaction costs - 20 bps per 100% 1-W turnover and 100 bps per 100% 1-W turnover. The first case corresponds to the worst case observed historically for the large and mid cap universe of the indices while the second case assumes 80% reduction in market liquidity and a corresponding increase in transaction costs. The statistics are calculated over the period from 29/06/1970 to 21/12/2012.

| USA Lo | ong-Term Track Records | Max Decon. | Div. Risk Weighted | Max Decorr. | Efficient Minimum Volatility | Efficient Maximum Sharpe Ratio | Cap- Weighted |
|--------------------|--|------------|-----------------------|----------------|------------------------------------|---|------------------|
| | Annualised return | 12.77% | 12.83% | 12.76% | 13.00% | 12.86% | 10.45% |
| | Annualised volatility | 17.18% | 16.40% | 16.52% | 14.03% | 15.68% | 17.12% |
| | Ann. 1-way turnover | 23.48% | 25.67% | 59.51% | 54.81% | 65.02% | 2.59% |
| Before Turnover | Annualised return net of 20bps transaction costs | 12.72% | 12.78% | 12.64% | 12.89% | 12.73% | 10.44% |
| Control | Annualised return net of 100bps transaction costs | 12.54% | 12.57% | 12.16% | 12.45% | 12.21% | 10.42% |
| | Days to Trade for \$1bn Initial Investment (95% Quantile)* | 0.10 | 0.11 | 0.12 | 0.13 | 0.11 | 0.03 |
| | Average float (US\$ bn) | 9.890 | 10.700 | 9.540 | 11.640 | 10.390 | 42.840 |
| | Annualised return | 12.59% | 12.67% | 12.61% | 12.69% | 12.93% | 10.45% |
| | Annualised volatility | 17.02% | 16.34% | 16.20% | 14.30% | 15.55% | 17.12% |
| | Ann. 1-way turnover | 20.19% | 22.15% | 29.22% | 29.83% | 27.84% | 2.59% |
| After Turnover | Annualised return net of 20bps transaction costs | 12.55% | 12.63% | 12.55% | 12.63% | 12.87% | 10.44% |
| Control | Annualised return net of 100bps transaction costs | 12.39% | 12.45% | 12.32% | 12.39% | 12.65% | 10.42% |
| | Days to Trade for \$1bn Initial Investment (95% Quantile)* | 0.10 | 0.11 | 0.12 | 0.13 | 0.12 | 0.03 |
| | Average float (US\$bn) | 10.110 | 10.860 | 10.120 | 12.030 | 10.820 | 42.840 |

^{*} Days To Trade is the number of days necessary to trade the total stock positions, assuming USD1bn AUM and that 100% of the Average Daily Dollar Traded Volume can be traded every day. Due to data availability, the period is restricted to the last 10 years of the sample for the Scientific Beta US indices.

Most interestingly, the reduction in turnover is accompanied by no, or at most a marginal, loss in returns and volatility reduction. Indeed, the reduction in turnover of the five strategies analysed (respectively Maximum Deconcentration, Diversified Risk Weighted, Maximum Decorrelation, Efficient Minimum Volatility and Efficient Maximum Sharpe ratio indices) are marginally changed from respectively 12.77% to 12.59%, 12.83% to 12.67%, 12.76% to 12.61%, 13% to 12.69% and 12.86% to 12.93% (which is even an increase in returns). In parallel, the changes in volatilities are also very small. In short, reducing the turnover does not alter the benefits of Scientific Beta strategies over the long run to a significant extent, and brings implementation costs down substantially.

Capacity constraints

Capacity is a key ingredient in the constitution and construction of an equity index. To achieve it, adjustments in stock weights can be implemented post-optimisation, primarily with the use of cap-weight multipliers. The principle used to make such adjustments is to impose a threshold for the weight of a stock and for the weight change at rebalancing, relative to the market-cap-weight of the stock in its universe. Specifically, we define the cap-weight multipliers rules as follows:

Holding capacity constraints: Each stock weight is capped at a multiple of 10 of its free-float-adjusted market-capweight to avoid big investment in the smallest stocks.

Trading capacity constraints: Change in weight of each stock is capped to its free-float-adjusted market-cap-weight to

avoid large rebalancing in small stocks.6

As shown in Exhibit 2, the capacity constraints do not have a substantial impact on overall performance and turnover metrics over the selection of indices. The Scientific Beta US Maximum Decorrelation Index exhibits an estimated number of days to trade at 95% of 0.12 days and an average market capitalisation of US\$10.12bn before the capacity constraints are applied. These figures are marginally improved to 0.10 days to trade and US\$10.17bn average float after the capacity constraints are applied. Nevertheless, this marginal shift in performance and liquidity is one side effect of the capacity constraints, which are primarily designed to address deviations in weights of smaller cap stocks between the index and its capweighted reference. Indeed, it has been highlighted e.g. in Goltz and Gonzalez

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⁶ After capping weights and weight changes following the two adjustments, index weights are renormalised so they sum again to one. As a consequence, the effective multiple will change again and, eventually, the index can hold some stocks at a higher multiple of their cap-weight

Article 4

Exhibit 2: Comparison of performance, turnover and capacity before and after capacity adjustments.

The first panel reports the statistics for the indices before any capacity constraint is applied, whereas the second panel reports the statistics for the indices after capacity constraints are applied. The annualised 1-way turnover and average float is calculated at the end of each quarter. The turnover and average float figures reported here are the average of the annualised 1-way turnover and average float over the analysis period. The statistics are calculated over the period from 29/06/1970 to 21/12/2012.

| USA Lon | ng-Term Track Records | Max Decon. | Div. Risk Weighted | Max Decorr. | Efficient Minimum Volatility | Efficient Maximum Sharpe Ratio | Cap- Weighted |
|----------------------------|--|------------|-----------------------|----------------|------------------------------------|---|------------------|
| | Annualised return | 12.59% | 12.67% | 12.61% | 12.69% | 12.93% | 10.45% |
| | Annualised volatility | 17.02% | 16.34% | 16.20% | 14.30% | 15.55% | 17.12% |
| | Ann. 1-w turnover | 20.19% | 22.15% | 29.22% | 29.83% | 27.84% | 2.59% |
| Before capacity constraint | Days To Trade for \$1bn Initial Investment (Quantile 95%)* | 0.10 | 0.11 | 0.12 | 0.13 | 0.12 | 0.03 |
| | Average float (US\$bn) | 10.110 | 10.860 | 10.120 | 12.030 | 10.820 | 42.840 |
| | Index to Cap-Weight Ratio (Low Cap Decile) | 14.42 | 11.10 | 15.78 | 9.80 | 12.77 | 1 |
| | Annualised return | 12.63% | 12.70% | 12.67% | 12.73% | 12.98% | 10.45% |
| | Annualised volatility | 17.13% | 16.45% | 16.34% | 14.42% | 15.67% | 17.12% |
| | Ann. 1-w turnover | 20.20% | 22.15% | 29.23% | 29.84% | 27.85% | 2.59% |
| After capacity constraint | Days To Trade for \$1bn Initial Investment (95% Quantile)* | 0.10 | 0.11 | 0.10 | 0.12 | 0.11 | 0.03 |
| | Average float (US\$bn) | 10.160 | 10.910 | 10.170 | 12.080 | 10.880 | 42.840 |
| | Index to Cap-Weight Ratio (Low Cap Decile) | 9.66 | 8.31 | 8.55 | 6.35 | 7.67 | 1 |

*Days To Trade is the number of days necessary to trade the total stock positions, assuming USD1bn AUM and that 100% of the Average Daily Dollar Traded Volume can be traded every day. Due to data availability, the period is restricted to the last 10 years of the sample for the Scientific Beta US indices.

(2013) that smart beta indices can exhibit a bias toward smaller cap stocks relative to their cap-weight reference.

Exhibit 2 shows that the capacity constraint has a big impact on the ratio decile weight of index and decile weight of CW, especially in the "low market cap" decile. For example, in the case of the Scientific Beta US Maximum Deconcentration Index, weights before adjustments are equally distributed to each market capitalisation bucket. The ratio between sum of weights of the Maximum Deconcentration Strategy to cap deciles and sum of cap-weights in the "Low Market Cap" decile, where the Maximum Deconcentration strategy tends to concentrate 14.42 times more than the cap-weighted index on average historically, is above the 10-multiple threshold set in the capacity rule 1 explained earlier. Hence the adjustment observed on the "low" decile. After applying the capacity constraint, we observe the ratio has decreased to 9.66, respecting the capacity holding constraint.

Conclusion

In this article we have described the different aspects of implementation management and cost control. In

particular, we have shown how the adjustments have specific impacts on key target implementation metrics. The article shows that, even over long-term horizons, a very reasonable ex-post turnover level that is in line with the exante targets can be maintained with the use of a threshold-based method. The average annual one-way turnover of the indices we presented was reduced from 46% to 26% through the turnover rules, a level which is shown to have a small impact on the performance.

The capacity constraints allow us to manage the deviations from the cap-weighted reference index in terms of individual component market capitalisation both at the trading and the holding levels. Notably, we showed how the capacity constraint has an impact on controlling the imbalance between the weight allocated to smaller market cap stocks and their corresponding cap-weight, from, on average across the analysed indices, a 12.77 ratio to an 8.11 ratio.

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References

- Amenc, N., F. Goltz and A. Lodh. 2012.
 Choose Your Betas: Benchmarking
 Alternative Equity Index Strategies. Journal of Portfolio Management 39(1): 88-111.
- Amenc, N., F. Goltz and L. Martellini. 2013. Smart Beta 2.0. EDHEC-Risk Position Paper.
- Amenc, N., F. Goltz, L. Martellini and P. Retkowsky. 2011. Efficient Indexation: An Alternative to Cap-Weighted Indices. Journal of Investment Management 9(4): 1-23.
- Amenc, N., F. Goltz, N. Gonzalez and A. Thabault. May 2014. Investability of Scientific Beta Indices. ERI Scientific Beta White Paper Series.
- Goltz, F. and N. Gonzalez. 2013. Risk Managing Smart Beta Strategies. ERI Scientific Beta White Paper Series.
- Leland, H. 1999. Optimal Asset Rebalancing in the Presence of Transaction Costs. U.C. Berkeley University Working Paper.
- Martellini, L. and P. Priaulet. 2002.
 Competing Methods for Option Hedging in the Presence of Transaction Costs. *Journal* of Derivatives 9(3): 26-38.

Relative and Absolute Robustness of Smart Beta Strategies

By Felix Goltz, Ashish Lodh and Sivagaminathan Sivasubramanian

Iternative forms of equity indices, which draw from a wide range of portfolio construction practices, have become popular in recent years. The smart beta indices are usually marketed on the basis of outperformance. However more often than not, the issue of robustness, as in extreme risk and performance attribution to well-defined risk factors, is not dealt with by index providers. The results of an EDHEC-Risk Alternative Equity Beta Survey show that investors are wary of the robustness of outperformance provided by various smart beta strategies.⁷

In general, robustness refers to the capacity of a system to perform effectively in a constantly changing environment. In the context of smart beta strategies, two kinds of robustness need to be taken into account – relative robustness and absolute robustness.

A strategy is assumed to be 'relatively robust' if it is able to deliver similar outperformance in similar market conditions. Single factor indices aim to achieve this kind of robustness. For example, a value factor index is expected to outperform in times when the value factor is rewarded in the market and will underperform when the factor undergoes short-term losses. The value factor index would be deemed relatively robust if it aligns well with the value factor performance and does not suffer idiosyncratic losses due to any other causes including, but not limited to, stockspecific and sector-specific events.

Absolute robustness is the capacity of the strategy to deliver risk-adjusted performance in the future to a degree that is comparable with that of the past owing to a well-understood economic mechanism rather than by just chance. In other words, absolute robustness is the absence of pronounced state and/or

time dependencies and a strategy shown to outperform irrespective of prevailing market conditions can be termed robust in absolute terms.

Potential causes of lack of robustness

Lack of robustness in smart beta strategies is mainly caused by exposure to four different risks in the strategy construction process – factor fishing, model mining, non-robust weighting schemes and strong factor dependencies.

Factor Fishing Risks -

Investors who wish to benefit from factor premia need to address robustness when selecting a set of factors. Harvey et al. (2013) document a total of 314 factors with a positive historical risk premium, showing that the discovery of the premium could be a result of data mining, i.e. strong and statistically significant factor premia may be a result of many researchers searching through the same dataset to find publishable results. For example, when capturing the value premium one may use extensive fundamental data including not only valuation ratios but also information on, for example, the sales growth of the firm. Therefore, a key requirement in investors accepting factors as relevant in their investment process is that there is a clear economic intuition as to why exposure to this factor constitutes a systematic risk (Kogan and Tian (2013)). Failure to recognise a suitable proxy for the rewarded factor will harm the relative robustness of the strategy.

Model Mining Risks -

Model mining risk is the risk of having an index construction methodology which results in a good track record in back testing. Many value-tilted indices include

a large set of ad-hoc methodological choices, opening the door to data mining. As an illustration, one can consider the impact of various specification choices on fundamental equity indexation strategies, which are commonly employed as a way to harvest the value premium.

Exhibit 1 summarises the maximum calendar year difference between any two variants of fundamental indices which make different choices for two methodological ingredients - variable selection and leverage adjustment. It is evident that the outperformance of a fundamental equity indexation strategy is highly sensitive to strategy specification choices.

The value factor performed poorly during the years 1999 and 2008. From a relative robustness viewpoint, two slightly different versions of a value-factortargeting smart beta strategy are expected to display similar performance in those two years. The results show, however, that 'total leverage adjusted' portfolio returns are up 5.3% while 'operating leverage adjusted' portfolio returns are down -4.0%, indicating that the weighting scheme does not reliably capture the value premium. In addition to being exposed to the value factor, the strategy is also exposed to some latent undesired risks resulting from proprietary definitions.

Non-Robust Weighting Schemes -

All smart beta strategies are exposed to unrewarded strategy-specific risks. Specific risks correspond to all the risks that are unrewarded in the long run, and therefore not ultimately desired by the investor. In line with portfolio theory, among the non-rewarded risks we find *specific financial risks* (also called idiosyncratic stock risks) which correspond to the risks that are specific to the company itself. It is this type of

Among the reasons for not investing in Smart Beta strategies, "doubts over robustness of outperformance" is rated the highest (Badaoui et al. (2014)).

Exhibit 1: Impact of Data Mining

The exhibit shows the returns of best and worst performing variants of each specification of the fundamental weighting schemes on the universe of the top 1000 US stocks. Portfolios are formed using fundamental data from the period January 1982 to December 2010. Data is obtained from Datastream and Worldscope.

| Data Mining aspects and their impact on returns | Best Performance | | Worst Per | formance | Range | Year |
|---|------------------|--------|--------------------|----------|-------|------|
| Variable Selection | Earnings | -12.2% | Dividends | -23.0% | 10.8% | 1999 |
| Leverage Adjustment | Total leverage | 5.3% | Operating leverage | -4.0% | 9.3% | 2008 |

risk that asset managers are supposed to be the best at recognising, evaluating and choosing in order to create alpha, but portfolio theory considers it to be neither predictable nor rewarded, so it is better to avoid it by investing in a well-diversified portfolio.

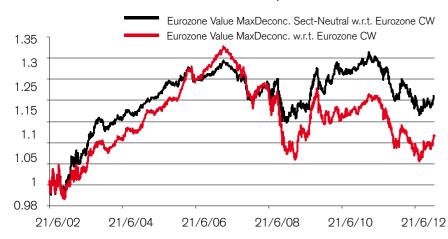
Specific risks can also correspond to important financial risk factors that do not explain, over the long term, the value of the risk premium associated with the index. The academic literature considers for example that commodity, currency, and sector risks do not have a positive long-term premium. For example, value strategies often lead to pronounced tilts towards financial sector stocks. During the financial crisis (2008), exposure to the financial sector proved to be a major determinant of the performance of these strategies. It should be noted that the tilt towards the financial sector may not be desired, but it came as a byproduct of holding value stocks. Exhibit 2 shows a performance comparison between the Eurozone Value Maximum Deconcentration8 index and its sectorneutral version. The Eurozone Value Maximum Deconcentration index overweighted the financial sector by 9.1% in June 2008, which resulted in a loss of about 20% of portfolio value.

Model-specific risks that are specific to the implementation of the diversification model are also a form of non-rewarded risk. As per Modern Portfolio Theory (MPT), each investor should optimally combine risky assets so as to achieve highest possible Sharpe ratio. Implementing this objective, however, is a complex task because of the presence of estimation risk for the required parameters, namely expected returns and covariances. In practice, the costs of estimation error may entirely offset the benefits of optimal portfolio diversification (DeMiguel, Garlappi and Uppal (2009) provide evidence that naively-diversified portfolios have higher out-of-sample Sharpe ratios than scientifically-diversified portfolios). In other words, the choice in risk and return parameter estimation for efficient diversification is between "trying," which has a cost related to estimation

Exhibit 2: Performance of Scientific Beta Eurozone Value Maximum Deconcentration and Sector-Neutral version during the financial crisis.

The benchmark is the cap weighted index on the Scientific Beta Eurozone universe, which consists of 600 stocks.

Relative Cumulative Returns with respect to CW Benchmark



risk, i.e. the risk of a substantial difference between the estimated parameter value and the true parameter value, or "giving up," which has a cost related to optimality risk, that is the risk that the heuristic benchmark (such as minimum volatility or equal-weighted) can be far removed from the optimal Maximum Sharpe ratio (MSR) benchmark.

Different portfolios are intuitively expected to incur more estimation risk or more optimality risk. Martellini, Milhau and Tarelli (2013) provide a quantitative analysis of the trade-off between optimality risk and estimation risk. They show that under the assumption of true parameter knowledge, an MSR portfolio exhibits a far superior Sharpe ratio to that of other strategies. But after estimation risk is taken into account, GMV and a mix of GMV and EW portfolios generate higher average Sharpe ratios.

The failure to avoid unrewarded strategy-specific risk hampers the relative robustness of the strategy, i.e. the strategy might not benefit to the maximum even in periods when the underlying risk factor is rewarded.

Dependency on Individual Factor Exposures –

Systematic risks come from the fact that smart beta strategies can be more or less exposed to particular risk factors, depending on the methodological choices guiding their construction (implicit), but also on the universe of stocks supporting this construction scheme (explicit). For example fundamental-weighted portfolios typically have a value tilt and minimum volatility strategies exhibit a low-beta tilt (see for example Scherer (2011), Blitz and Swinkels (2008), and Amenc, Goltz and Le Sourd (2008)). Each weighting scheme exposes investors to implicit risk factors which may or may not be consistent with their risk objective.

This is a major limitation of Smart Beta 1.0 strategies – the strategies which do not explicitly control for systematic risk factors. Following this drawback of Smart Beta 1.0 indices, 'factor indices' have

gained popularity. Factor indices make sure that the portfolio is tilted towards the desired risk factor. Whatever the route to seeking systematic risk exposure, the elementary fact remains that stocks earn a risk premium through their exposure to certain rewarded factors (Ross [1976]).9

Exhibit 3 plots cumulative returns of long/short cap-weighted indices replicating factors such as market, size, value and momentum. Periods of poor performance in all factors are common throughout the forty-year time horizon and the underperformance occurs at different points in time. Therefore investing in a single factor is not a robust approach in absolute terms, as the performance will vary greatly across different time periods.

Improving robustness

ERI Scientific Beta proposes three ways by which the robustness of various smart beta strategies can be improved.

Avoidance of Data Mining through a Consistent Framework –

A very effective mechanism to avoid data

mining is by establishing a consistent framework for smart beta index creation, thus limiting the choices yet providing the flexibility needed for smart beta index creation. Consistency in the index framework has two main benefits. First, it prevents model mining by limiting the number of choices through which indices can be constructed. A uniform framework is the best safeguard against *post hoc* index design, or model mining (i.e. the possibility to test a large number of smart beta strategies, and publish the ones that have good results).

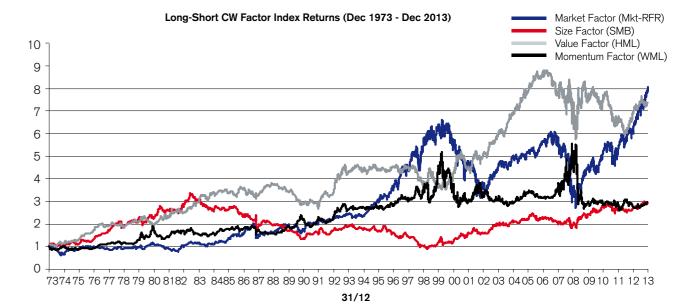
Second, analysis across specification choices is vital because the range of outcomes gives a more informative view than a single specification, which could always have been picked. An index that performs well across multiple specification choices is more robust than an index that performs only in a single specification choice, which could very well have been by chance rather than because of the robustness of the strategy. Pre-packaged indices do not allow investors to allow comparison across specifications to obtain a view on the sensitivity of performance

to index specification choices, thereby exposing investors to a risk of unintended consequences of undesired risks.ERI Scientific Beta uses a consistent smart beta index design framework for the construction of its entire set of smart beta indices known as the Smart Beta 2.0 approach. Stock selection allows investors to choose the right (rewarded) risk factors to which they want to be exposed. A well-diversified weighting scheme provides efficient access to the risk premia associated with this factor exposure. All the available variations (or choices) provided within the framework are based on proven academic or applied research allowing flexibility to accommodate various investor preferences. Exhibit 4 shows ERI Scientific Beta's design framework.

Exhibit 5 compares the design framework of the factor-based strategy indices offered by MSCI and ERI Scientific Beta. MSCI follows different stock selection schemes, weighting schemes and risk control options for different risk factors. Maximising the exposure to a factor by selecting stocks

Exhibit 3: Cumulative Returns of Long/Short Cap-Weighted Factors

The Market factor is the daily return of the cap-weighted index of all stocks that constitute the index portfolio in excess of the risk-free rate. The Small Size factor is the daily return series of a cap-weighted portfolio that is long the cap-weighted market portfolio deciles 6-8 (NYSE, Nasdaq, and AMEX) and short the 30% largest market-cap stocks from the top 500 stock universe. The Value factor is the daily return series of a cap-weighted portfolio that is long the 30% highest and short the 30% lowest B/M ratio stocks in the S&P 500 universe. The Momentum factor is the daily return series of a cap-weighted portfolio that is long the 30% highest and short the 30% lowest 52 weeks (minus the most recent 4 weeks) past return stocks of the US 500 universe. The "Secondary Market US Treasury Bills (3M)" is the risk-free rate in US Dollars. The analysis is based on daily total return data from 31 December 1973 to 31 December 2013 (40 years). The complete stock universe consists of the 500 largest stocks in the USA. The S&P 500 index is used as the cap-weighted benchmark.



The economic intuition for the existence of a reward for a given risk factor is that exposure to such a factor is undesirable for the average investor because it leads to losses in bad times (i.e. when marginal utility is high, see Cochrane (2001)).

⁸ Maximum Deconcentration is an equal weighting (1/N) strategy with liquidity and turnover constraints.

Exhibit 4: ERI Scientific Beta's Consistent Index Design Framework Weighting Geography Stock selection scheme **Risk Control Options** (factor tilt) (diversification method) United States Large Cap Max Deconcentration • 2% TE/CW • 3% TE/CW Eurozone Mid Cap Max Decorrelation United Kingdom High Volatility Efficient Min Volatility • 5% TE/CW • Developed Europe ex. UK Low Volatility • Efficient Max Sharpe Geo Neutral Japan Value + High • Div. Risk Weighted • Sector Neutra Liquidity • Div. Multi-Strategy • Dev. Asia Pacific ex. Japan Growth • High Momentum • Developed ex. UK • Developed ex. US Low Momentum Developed • High Dividend Yield Low Dividend Yield High Liquidity Mid Liquidity

| Factor | Index | Stock selection | Weighting Scheme | Risk controls | |
|----------|---|---|---|--|--|
| | | MSCI Index Methodologie | s | | |
| Size | MSCI Equal-Weight Index | All stocks in CW parent index universe | Equal-weighted | None | |
| Value | MSCI Value-weighted index | All stocks in CW parent index universe | Score adjusted by investability factor | None | |
| Mom. | MSCI Momentum Index | Selection by momentum score (fixed number of constituents to target 30% market cap coverage) | Market cap * momentum score | Cap on weight of individual security | |
| Low Vol. | MSCI Minimum Volatility Index | All stocks in CW parent index universe | Optimisation to minimise portfolio risk | Sector and country weight constraints Cap on multiple of market cap of individual security | |
| Yield | MSCI High Dividend Yield Index | Select stocks with dividend yield > 1.3x parent index dividend yield | Market cap weighted | Cap on weight of individual security | |
| | Sci | ientific Beta Index Methodol | logies | | |
| Size | SciBeta Div. Multi-Strategy Mid Cap Index | | | | |
| Value | SciBeta Div. Multi-Strategy Value Index | | | | |
| Mom. | SciBeta Div. Multi-Strategy High Momentum Index | Half the stocks by relevant | Same weighting scheme for selected stocks | Cap on multiple of | |
| Low Vol. | SciBeta Div. Multi-Strategy Low Volatility Index | score | (Diversified Multi-Strategy by default) | market cap and weight of individual securities | |
| Yield | SciBeta Div. Multi-Strategy High Dividend Yield Index | | | | |

that are most exposed to the desired risk factor and the application of a capweighting scheme to this selection (MSCI High Dividend Yield) does not attend to the problem of poor diversification arising from high concentration. Weighting either the whole of the universe (MSCI Value) or a part of the universe (MSCI Momentum) by exposure to this factor, resulting in score/rank weighting, also misses out on diversification.

The Smart Beta 1.0 approach to a factor index (MSCI Minimum Volatility) does not guarantee either the highest exposure

to low-volatility stocks or optimal diversification of this low-volatility portfolio. Moreover, it brings about other kinds of undesired risks, such as exposure to defensive sectors. Similarly, seeking exposure to the size factor through equal weighting of a broad universe is certainly less effective than selecting the smallest size stocks in the universe and then diversifying them, including with an equal-weighted weighting scheme. Also, no control for the undesired liquidity risk is implemented. Not only is the approach not optimal from the standpoint

of a well diversified factor index, but the lack of uniformity in index design across factor indices may also introduce the data mining bias described earlier.

Another approach to the inconsistency of the conceptual framework, in addition to comparing construction methods for different factors as we did for MSCI, is by looking at the evolution or change of methodology over time for the same strategy or the same factor. Russell launched new factor indices to create a new brand known as 'High Efficiency' (HE) indices when it already had the

following factor indices on the market – Russell 1000 High Momentum, Russell 1000 Low Volatility and Russell 1000 Value. The new indices have the same objective as the old ones but different construction principles.

Exhibit 6 shows the performance difference between the new set and the old set of Russell indices. Thus, an inconsistent framework (over time) is also a kind of model mining that allows index providers to launch new indices with better track records than the previous.

Improving Relative Robustness by Reducing Unrewarded Risks –

Relative robustness can be improved by minimising the unrewarded risk as much as possible. Among these unrewarded risks, fifty years of research in finance and financial econometrics have aimed to reduce model-specific risk, notably errors in estimating the parameters used in the weighting schemes. There are numerous approaches to the estimation of risk parameters. The sample estimator of the covariance matrix produces extremely high estimation errors when the ratio of universe size to sample size is large (Kan and Zhou (2007)) – sample risk. One solution to this problem is to reduce the number of parameters to be estimated by imposing a structure on the covariance matrix (Chan et al. (1999)). Although this method reduces sample risk, its drawback is that the estimator is biased if the risk model does not conform to the true stock return generating process - model risk.

The next generation of estimators aim to achieve a trade-off between sample

risk and model risk by combining sample estimators and structured estimators (Ledoit and Wolf (2003)). Another way to reduce model risk, which is used by ERI Scientific Beta, and not necessarily at the cost of sample risk, is to use an implicit factor model such as principal component analysis (PCA). The factors from the PCA have the benefit of being uncorrelated and of providing the best summary of the information contained in the dataset (i.e. zero model risk).

To reduce sample risk, the number of statistical factors is limited using a criterion from Random Matrix Theory in order to achieve parsimony and robustness (Plerou *et al.* (2002)). Coqueret and Milhau (2014) show that minimum volatility strategies using Principal Component (PC) tend to have lower volatilities compared to other estimation techniques.

One serious concern with optimisationbased weighting schemes, is that the stocks with the highest estimation error may receive the highest weight—a process commonly known as "Error Maximisation"—which is detrimental to the relative robustness of strategies. ERI Scientific Beta uses two types of constraints to improve diversification—a long-only constraint and a deconcentration constraint. Jagannathan and Ma (2003) provide empirical evidence that imposing non-negativity constraints removes large outliers and hence provides better performance through better diversification. Deconcentration constraints ensure sufficiently balanced weights across constituents. 10

DeMiguel et al. (2009) introduce flexible quadratic constraints that put limits on the overall amount of concentration in the portfolio (e.g. on the sum of squares of portfolio weights) rather than limiting the weight of each stock in the portfolio, thus leaving more room for the optimiser while avoiding concentration overall. ERI Scientific Beta applies norm constraints for the minimum-volatility weighting scheme by placing a lower bound on the effective number of stocks of the portfolio -Neff.¹¹ This method was chosen for the minimum volatility approaches because they are very sensitive, due to their natural concentration in low-volatility stocks, to the definition of maximum and minimum weights. We felt it was less arbitrary to use the effective number of stocks, which would avoid an in-sample weighting constraint risk and would give a greater role in the weighting scheme to the proper use of the diversification properties of minimum volatility.

Even though the different weighting schemes offer efficient diversification of stocks, there is an additional need for diversification of the weighting schemes to diversify away the strategy-specific risks—a concept called "Diversifying the Diversifiers." ERI Scientific Beta proposes Diversified Multi-Strategy—an equal combination of five weighting schemes—as its flagship strategy for factor indices. The combination of different strategies allows diversification of risks that are specific to each strategy by exploiting the imperfect correlation between the different strategies'

Exhibit 6: Russell Factor Indices Performance Comparison

All statistics are annualised and daily total returns are used for the analysis.

| All statistics are annualised and daily total returns are used for the analysis. | | | | | | | | |
|--|---|--------------------------------|-------------------|----------------------|--------------|--|--|--|
| USA Russell Factor Indices | Methodology | Time Period | Annual Returns | Annual Volatility | Sharpe Ratio | | | |
| Russell 1000 High Efficiency Momentum | Tilt the portfolio based on Momentum score taking market cap weight of stock in the Russell 1000 Index as starting point. | 01/01/2005 to 31/12/2013 | 8.69% | 21.62% | 0.33 | | | |
| Russell 1000 High Momentum | Cap weight up to 200 highest momentum stocks in Russell 1000 Index. | 31/12/2013 | 8.05% | 20.59% | 0.31 | | | |
| Russell 1000 High Efficiency Low Volatility | Tilt the portfolio based on Low Volatility score taking market cap weight of stock in the Russell 1000 Index as starting point. | 01/01/2005 to 31/12/2013 | 7.89% | 17.73% | 0.36 | | | |
| Russell 1000 Low Volatility | Cap weight up to 200 least volatile stocks in Russell 1000 Index. | 31/12/2013 | 7.69% | 16.35% | 0.37 | | | |
| Russell 1000 High Efficiency Value | Tilt the portfolio based on Value score (B/M and E/P ratios) taking market cap weight of stock in the Russell 1000 Index as starting point. | 31/12/2003 | 9.76% | 22.55% | 0.36 | | | |
| Tilt the portfolio based on Value | | to 31/12/2013 | 7.56% | 21.96% | 0.27 | | | |



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parameter estimation errors. Thus, diversifying the model risks further reduces the unrewarded risks and renders the weighting scheme more robust (in a relative manner).

Improving Absolute Robustness by Diversifying across Factors -

Investors who rely on a single factor exposure take the risk of the underlying factor underperforming over short periods. The reward for exposure to these factors has been shown to vary over time (see e.g. Harvey (1989), Asness (1992), Cohen, Polk and Vuolteenaho (2003)). While this time variation in returns is not completely in sync for different factors, allocating across factors allows investors to diversify the sources of their outperformance and smooth their performance across market conditions. Exhibit 7 shows the correlation of the relative returns of factor-tilted multistrategy indices over a cap-weighted benchmark. The indices are not perfectly correlated with each other which shows a potential for diversification across factors in order to reduce risk and generate smoother outperformance over time.

ERI Scientific Beta offers two multibeta allocations - Equal Weight (EW) and Equal Risk Contribution (ERC). The Equal Weight allocation, which is a simple and robust allocation in terms of absolute risk, invests 1/4 in each of the four Multi-Strategy factor indices. The Equal Risk Contribution allocation combines the four Multi-Strategy factor indices so as to equalise their contributions to the tracking error risk.

Measurement of robustness

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ERI Scientific Beta proposes extreme risk measures including maximum relative

drawdown analysis and a factor attribution exercise as measures of relative robustness and outperformance probability and conditional performance as tools to assess absolute robustness.

The Maximum Relative Drawdown measures the maximum relative loss experienced by a strategy between a peak and a valley over a specified period. It is important to see if the losses can be explained through market fundamentals and if the reasons are in line with the index construction methodology. If not, then there are other unintended risks at play which bring down the relative robustness of the strategy. Exhibit 8 shows that maximum loss occurred during the late 1990s technology bubble when the capweighted benchmark was over-weighted in growth and technology stocks.

Many studies have underlined the importance of factor exposures in explaining part of the outperformance of portfolio strategies over cap-weighted indices (see Jun and Malkiel (2007) and Amenc, Goltz and Le Sourd (2008)). It is a particularly important robustness check in the case of single and multi-factor indices because it discloses what portion of a strategy's performance is indeed derived from its exposure to the intended risk factor and how much can be attributed to other factors and unexplained alpha. The attribution exercise can be extended to tracking error to monitor the role of each factor in the deviation of the strategy from its benchmark.

Since the performance of smart beta varies over time, the analytics reported over long horizons—for example excess returns over 40 years have limited information because of averaging over time periods. Probability of outperformance is a measure that

overcomes this limitation. The probability of outperformance is defined as the empirical frequency of outperforming the cap-weighted reference index over a given investment horizon. It is an intuitive and relevant measure which shows how often and consistently the strategy would be able to outperform the cap-weighted reference index in the past for all possible entry points. Exhibit 10 shows the probability of outperforming the cap-weighted benchmark of multi-beta multi-strategy EW, ERC and the simple average of the four component single beta indices with various investment horizons for two stock universes. This shows that a combination of factors indeed improves the chances of outperforming the CW benchmark (improves absolute robustness) compared to single factors in isolation.

Analysing the conditional performance of the smart beta strategies in bull-bear market conditions or in contractionexpansion business cycles is a powerful tool in robustness analysis because the performance of smart beta strategies is shown to vary over market phases (Gonzalez and Thabault (2013)). A strategy which performs well in different market conditions and shows little or no state and time dependency can be said to be robust in an absolute sense.

Exhibit 11 shows that multi-beta multi-strategy indices outperform the cap-weighted benchmarks in both the bull and bear regimes, whereas the component indices perform very differently in different market conditions. For example, the low-volatility index performs very poorly in bull markets but performs extremely well in bear markets and the mid-cap index performs well in bull markets but has a relatively poor information ratio in bear markets.

Exhibit 7: Correlation of Relative Returns (over CW index) across Factor-Tilted Multi-Strategy Indices

The analysis is based on daily total return data from 31 December 1973 to 31 December 2013 (40 years). The S&P 500 index is used as the cap-weighted benchmark.

| US Long Term (1974-2013) | | Diversified Multi-Strategy | | | | | | |
|-----------------------------|----------------|----------------------------|----------|---------|-------|--|--|--|
| | | Mid Cap | Momentum | Low Vol | Value | | | |
| | Mid Cap | 100% | 69% | 64% | 86% | | | |
| Diversified Multi- | Momentum | | 100% | 63% | 66% | | | |
| Strategies | Low Volatility | | | 100% | 71% | | | |
| | Value | | | | 100% | | | |

¹⁰ We impose an upper bound u_i and a lower bound l_i on the weight of each constituent security,

 $l_i = \frac{1}{3N} \le w_i^* \le u_i = \frac{3}{N}$

where i=1,...,N and N is the nominal number of constituents. Stock weights are bound to be below 3/N and above 1/3N, where N denotes the number of constituents.

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¹¹ $N_{eff} \ge \frac{N}{33}$ $N_{eff} = Effective Number of Stocks = <math>\frac{1}{N^N + N^2}$, where N is the number of constituent stocks in the index and W_i is the weight of stock i in the

¹² See Timmermann (2006), Kan and Zhou (2007), Tu and Zhou (2010) and Amenc, Goltz, Lodh, Martellini (2012) on the benefits of combining portfolio strategies.

Exhibit 8: Maximum Relative Drawdown Analysis

The analysis is based on daily total returns data from 31/12/1973 to 31/12/2013 (40 years). The S&P 500 is used as the cap-weighted benchmark. Maximum relative drawdown is the maximum drawdown of the long-short index whose return is given by the fractional change in the ratio of the strategy index to the benchmark index.

| IIC I and Tarm | Diversified Multi-Strategy | | | | | | | | |
|-----------------------------|----------------------------|------------|------------|------------|----------------------------------|-----------------------------------|--|--|--|
| US Long Term (1974-2013) | Mid Cap | Momentum | Low Vol | Value | Multi-Beta Multi- Strategy EW | Multi-Beta Multi- Strategy ERC | | | |
| Maximum Relative DD | 42.06% | 17.28% | 43.46% | 32.68% | 33.65% | 28.74% | | | |
| Start of Max Rel DD | 24/03/1994 | 23/03/1994 | 20/09/1993 | 22/03/1994 | 24/03/1994 | 25/03/1994 | | | |
| Maximum Loss Point | 27/03/2000 | 22/12/1999 | 10/03/2000 | 23/03/2000 | 27/03/2000 | 27/03/2000 | | | |
| Recovery Completed on | 06/09/2001 | 03/04/2001 | 06/09/2001 | 02/03/2001 | 04/04/2001 | 04/04/2001 | | | |

Exhibit 9: Exposure to Equity Risk Factors - Carhart

The complete stock universe consists of the 500 largest stocks in the USA. The Market factor is the daily return of the cap-weighted index of all stocks that constitute the index portfolio in excess of the risk-free rate. The Small Size factor is the daily return series of a cap-weighted portfolio that is long the smallest 30% of stocks (by market cap) and short the largest 30% of stocks (by market cap) of the extended universe (i.e. including small caps). The Value factor is the daily return series of a cap-weighted portfolio that is long the 30% highest and short the 30% lowest B/M ratio stocks in the investable universe. The Momentum factor is the daily return series of a cap-weighted portfolio that is long the 30% highest and short the 30% lowest 52 weeks (minus the most recent 4 weeks) past return stocks in the investable universe. The "Secondary Market US Treasury Bills (3M)" is the risk-free rate in US Dollars. All statistics are annualised. The analysis is based on daily total returns from 31/12/1973 to 31/12/2013. The statistics that satisfy a 95% significance level are highlighted in bold.

| UC Lang Tayes | Diversified Multi-Strategy | | | | | | | | |
|-----------------------------|----------------------------|----------|------------------|--------|----------------------------------|-----------------------------------|--|--|--|
| US Long Term (1974-2013) | Mid Cap | Momentum | Low Vol | Value | Multi-Beta Multi- Strategy EW | Multi-Beta Multi- Strategy ERC | | | |
| Annual Alpha | 2.66% | 1.84% | 2.85% | 2.33% | 2.45% | 2.35% | | | |
| Market Beta | 0.93 | 0.94 | 0.78 | 0.91 | 0.89 | 0.89 | | | |
| SMB Beta | 0.31 | 0.16 | 0.02 | 0.16 | 0.16 | 0.15 | | | |
| HML Beta | 0.16 | 0.09 | 0.14 | 0.31 | 0.17 | 0.16 | | | |
| MOM Beta | 0.00 | 0.17 | 0.00 | 0.03 | 0.05 | 0.06 | | | |
| R-Squared | 92.20% | 95.52% | 90.14% | 95.00% | 94.76% | 95.46% | | | |
| | | Per | formance Attribu | tion | | | | | |
| Unexplained (Alpha) | 3.22% | 2.44% | 3.23% | 2.90% | 3.02% | 2.91% | | | |
| Market Beta | 4.96% | 5.00% | 4.16% | 4.88% | 4.75% | 4.76% | | | |
| SMB Beta | 0.85% | 0.44% | 0.06% | 0.43% | 0.44% | 0.41% | | | |
| HML Beta | 0.80% | 0.44% | 0.71% | 1.56% | 0.88% | 0.80% | | | |
| MOM Beta | -0.01% | 0.46% | -0.01% | 0.08% | 0.13% | 0.15% | | | |

In conclusion, it is essential that smart beta strategy performance reporting be accompanied by a measurement of the relative and absolute robustness of its performance. The lack of relative robustness arises mainly from data mining. non-robust weighting methodologies and that of absolute robustness comes from undiversified factor exposures. Relative robustness can be improved by reducing all sources of unrewarded risks with the use of a consistent framework (to prohibit data mining), robust parameter estimation techniques, weight constraints, and strategy-specific risk. Absolute robustness can be achieved through allocating across several rewarded factors. Our results show that the single factor indices have a high degree of relative robustness, but they are not robust in absolute terms. The multibeta allocations on the other hand are highly robust in absolute terms. \blacksquare

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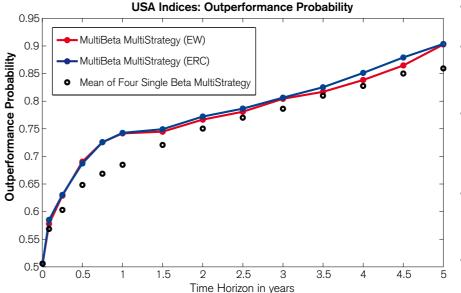
References

- Amenc, N., F. Goltz and V. Le Sourd. 2008.
 The Performance of Characteristics-based
 Indices. European Financial Management 15(2): 241–278
- Amenc N., F. Goltz., A. Lodh A. and L. Martellini. 2012. Diversifying the Diversifiers and Tracking the Tracking Error: Outperforming Cap-Weighted Indices with

- Limited Risk of Underperformance, Journal of Portfolio Management 38 (3): 72-88
- Asness, C. 1992. Changing Equity Risk Premia and Changing Betas over the Business Cycle and January. University of Chicago Working Paper.
- Badaoui, S., F. Goltz, V. Le Sourd and A. Lodh. 2014 (forthcoming). Alternative Equity Beta Investing: The Status Quo and the Path Ahead. EDHEC Risk Institute Publication.
- Blitz, D. and L. Swinkels. 2008. Fundamental Indexation: An Active Value Strategy in Disguise. *Journal of Asset Management* 9(4): 264-269.
- Chan, L. K. C., J. Karceski and J. Lakonishok. 1999. On Portfolio Optimization: Forecasting Covariances and Choosing the Risk Model. Review of Financial Studies 12(5): 937–974.
- Cochrane, J. H. 2001. Asset Pricing. Princeton University Press.

Exhibit 10: Outperformance Frequency over Different Horizons

The analysis is based on daily total return data from 31 December 1973 to 31 December 2013 (40 years). The S&P 500 is used as the cap-weighted benchmark. Probability of outperformance is the historical empirical probability of outperforming the cap-weighted benchmark over an investment horizon of 1 month, 3 months, 6 months, 9 months, 1 year, 18 months, 2 years, 36 months, and so on, up to 5 years irrespective of the entry point in time. It is computed using a rolling window analysis with window length corresponding to the investment horizon and one-week step size.



- Cohen, R. B., C. Polk and T. Vuolteenaho. 2003. The Value Spread. *Journal of Finance* 58(2): 609-642.
- Coqueret, G. and V. Milhau. 2014.
 Estimating Covariance Matrices for Portfolio
 Optimisation. EDHEC Risk Institute
 Publication.
- DeMiguel, V., L. Garlappi, F. Nogales and R. Uppal. 2009. A Generalized Approach to Portfolio Optimization: Improving Performance by Constraining Portfolio
- Norms. *Management Science* 55(5):798-812. Gonzalez, N. and A. Thabault. 2013.
- Overview of Diversification Strategies. ERI Scientific Beta White Paper.

 Harvey, C. R. 1989. Time-Varying
- Conditional Covariances in Tests of Asset Pricing Models. *Journal of Financial Economics* 24: 289-317.
- Harvey, C., Y. Liu, and H. Zhu. ... and the Cross-Section of Expected Returns. Working paper, Duke University, 2013.

- Jagannathan, R. and T. Ma. 2003. Risk Reduction in Large Portfolios: Why Imposing the Wrong Constraints Helps. *Journal of Finance* 58(4): 1651-1684.
- Jun, D. and B. Malkiel. 2007. New Paradigms in Stock Market Indexing. European Financial Management 14(1): 118–126.
- Kan, R. and G. Zhou. 2007. Optimal Portfolio Choice with Parameter Uncertainty. *Journal of Financial and Quantitative Analysis* 42(3): 621-656.
- Kogan, L., and M. Tian. Firm Characteristics and Empirical Factor Models: A Data-Mining Experiment. Working paper, MIT, 2013.
- Ledoit, O. and M. Wolf. 2003. Improved Estimation of the Covariance Matrix of Stock Returns with an Application to Portfolio Selection. *Journal of Empirical Finance*, 10: 603-621.
- Martellini, L., V. Milhau and A. Tarelli. 2013. Estimation Risk versus Optimality Risk: An Ex-Ante Efficiency Analysis of Heuristic and Scientific Equity Portfolio Diversification Strategies. EDHEC-Risk Institute Working Paper.
- Plerou, V., P. Gopikrishnan, B. Rosenow, L. Amaral, T. Guhr, H. Stanley. 2002. Random Matrix Approach to Cross Correlations in Financial Data. *Physical Review* E 65 (6): 066126
- Ross, S.A. 1976. The Arbitrage Theory of Capital Asset Pricing. *Journal of Economic* Theory 13: 341-360.
- Scherer, B. 2011. A Note On the Performance of the Minimum Variance Portfolio, Journal of Empirical Finance, p.652-660
- Timmermann, A. 2006. Forecast Combinations, Handbook of Economic Forecasting, Elsevier.
- Tu, J. and G. Zhou. 2010. Incorporating Economic Objectives into Bayesian Priors: Portfolio Choice under Parameter Uncertainty. *Journal of Financial and Ouantitative Analysis* 45(4): 959-986.

Exhibit 11: Conditional Performance

Calendar quarters with positive market index returns comprise bull markets and the rest constitute bear markets. All statistics are annualised. The analysis is based on daily total return data from 31 December 1973 to 31 December 2013 (40 years). The complete stock universe consists of the 500 largest stocks in the USA. The S&P 500 index is used as the cap-weighted benchmark.

| LIC Long Torm | Diversified Multi-Strategy | | | | | | | | |
|-----------------------------|----------------------------|----------|--------------|-------|----------------------------------|-----------------------------------|--|--|--|
| US Long Term (1974-2013) | Mid Cap | Momentum | Low Vol | Value | Multi-Beta Multi- Strategy EW | Multi-Beta Multi- Strategy ERC | | | |
| Bull Markets | | | | | | | | | |
| Annual Relative Returns | 5.12% | 3.28% | -0.99% | 3.54% | 2.79% | 2.71% | | | |
| Annual Tracking Error | 5.76% | 4.04% | 5.11% | 5.00% | 4.38% | 4.13% | | | |
| Information Ratio | 0.89 | 0.81 | -0.19 | 0.71 | 0.64 | 0.66 | | | |
| | | | Bear Markets | | | | | | |
| Annual Relative Returns | 3.83% | 3.77% | 8.12% | 5.99% | 5.49% | 5.14% | | | |
| Annual Tracking Error | 8.33% | 6.26% | 7.94% | 7.12% | 6.57% | 6.12% | | | |
| Information Ratio | 0.46 | 0.60 | 1.02 | 0.84 | 0.83 | 0.84 | | | |

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Assessing Factor Indices

By Felix Goltz and Ashish Lodh

his article provides a brief overview of equity factor index offerings from major index providers. Factor indices aim to provide explicit exposure to a common risk factor to harvest its long-term risk premia. Due to the predominance of long-only indices in practical application, we focus here on long-only indices and do not include long/short index offerings. To get a synthetic view on the performance of different factor indices, we have included one index each from the following index providers: ERI Scientific Beta, MSCI, Russell, FTSE and FTSE RAFI.

Index construction methodology

Traditional factor indices fall into two major categories. The first involves maximising the exposure to a factor by selecting stocks that are most exposed to the desired risk factor and the application of a cap-weighting (CW) scheme to this selection. This approach is included in the illustrations in the form of Scientific Beta tilted CW indices. While this approach brings the exposure to the desired factor, the problem of poor diversification arising from high concentration in a small number of stocks remains unanswered. The second method weights either the whole of the universe (Russell factor indices) or a part of universe (MSCI Momentum) by the exposure to this factor, resulting in score/rank weighting. Here again, the maximisation of the factor exposure does not guarantee that the indices are well diversified.

To overcome these difficulties, index providers that generally offer factor indices on the basis of the first two approaches have recently sought to take advantage of the development of smart beta indices to offer investors a new framework for smart factor investing (Bender *et al.* (2013)). This approach recognises that smart betas have implicit risk exposures and aims to select and combine them according to these

varying exposures. The drawback of this approach is that it maximises neither factor exposure nor diversification of the indices. For example, a minimum volatility index on a broad universe (e.g. MSCI Minimum Volatility) does not guarantee either the highest exposure to low-volatility stocks or the best diversification of this low-volatility portfolio.

Factor indices
aim to provide
explicit exposure to a
common risk factor to
harvest its long-term
risk premia.

Similarly, seeking exposure to the size factor through equal weighting of a broad universe is certainly less effective than selecting the smallest size stocks in the universe and then diversifying them, including with an equal-weighted weighting scheme. Finally, seeking to be exposed to the value factor through a value-weighted index (for e.g. FTSE RAFI 1000 series and MSCI Value) will not produce a well-diversified index, simply because the integration of the attributes characterising the value exposure into the weighting does not take the correlations between these stocks into account.

In view of these problems, EDHEC-Risk Institute has promoted the concept of smart factor investing using the Smart Beta 2.0 approach. The idea is to construct a factor-tilted portfolio

to extract the factor premia most efficiently and is based on two pillars: 1) explicitly selecting appropriate stocks for the desired beta and 2) using a diversification-based weighting scheme (Amenc et al. (2013)). ERI Scientific Beta constructs smart factor indices by using diversified multi-strategy weighting on characteristics-based half universes - small size, high momentum, low volatility, and value.¹³ In particular, the indices use a Diversified Multi-Strategy weighting, which consists of an equal allocation to the five following weighting schemes: Maximum Deconcentration, Risk Weighted, Maximum Decorrelation, Minimum Volatility and Maximum Sharpe Ratio.

This article performs a comparative study across major providers of factor indices – MSCI, Russell, FTSE, and FTSE RAFI. S&P offers factor indices in USA and FTSE RAFI recently launched a Low Volatility index series, but due to limited history of publicly available data (less than 10 years) on these indices, we have not included them in the analysis, because it is not possible for us to draw conclusions from periods that are too short.

It should be noted that different index providers include implementation rules in their indices in order to avoid transaction costs for investors trying to capture the factor exposures. Russell indices have an implicit reference to market cap weights, which naturally tends to ease implementation. The MSCI factor indices use different rules across different factors. For example, no investability adjustments are made for equal-weighted indices. Other factor indices use different adjustments such as a weight cap in the momentum index, turnover constraints in the minimum volatility index, and smoothing over average fundamental variables in the value-weighted indices. The ERI Scientific Beta indices apply investability rules (capacity and turnover control) as well as turnover constraints.14

| Factor | 1: An overview of factor index con Index | Stock selection | Weighting Scheme | Risk controls | | | | | |
|---------------------------|--|---|--|--|--|--|--|--|--|
| ractor | IIIUEX | MSCI Index Methodology | Weighting Scheme | RISK COILLOIS | | | | | |
| Size | MSCI Equal-Weight Index | All stocks in CW parent index universe | Equal-weighted | None | | | | | |
| Value | MSCI Value-weighted index | All stocks in CW parent index universe | Score adjusted by investability factor | None | | | | | |
| Mom. | MSCI Momentum Index | Selection by momentum score (fixed number of constituents to target 30% market cap coverage) | Market cap * momentum score | Cap on weight of individual security | | | | | |
| Low Vol. | MSCI Minimum Volatility Index | All stocks in CW parent index universe | Optimisation to minimise portfolio risk | Sector and country weight constraints Cap on multiple of market cap of individual security | | | | | |
| | · | Scientific Beta Index Methodology | | | | | | | |
| Size | SciBeta Div. Multi-Strategy Mid Cap Index | | Same weighting | | | | | | |
| Value | SciBeta Div. Multi-Strategy Value Index | | scheme for selected | Cap on multiple of market cap and weight of individual securities | | | | | |
| Mom. | SciBeta Div. Multi-Strategy High Momentum Index | Half the stocks by relevant score | stocks (Diversified Multi-Strategy by | | | | | | |
| Low Vol. | SciBeta Div. Multi-Strategy Low Volatility Index | | default) | | | | | | |
| Russell Index Methodology | | | | | | | | | |
| Size | Russell Mid Cap Index | Smallest 800 companies from parent index | Cap-Weighted | None | | | | | |
| Value | Russell High Efficiency Value | Scoring based on Non Linear Probability method, results in approximately 50% of the stocks of the CW parent index | Conversion of the scores calculated in | Turnover | | | | | |
| Mom. | Russell High Efficiency Momentum | Scoring based on Non Linear Probability method, results in approximately 50% of the stocks of the CW parent index | the stock selection stage into active weights by using the | minimisation by calculating new stocks' weights | | | | | |
| Low Vol. | Russell High Efficiency Low Vol | Scoring based on Non Linear Probability method, results in approximately 30% of the stocks of the CW parent index | NLP method using cap-weights as base. | using a banding process | | | | | |
| | | FTSE Index Methodology | | • | | | | | |
| Size | FTSE Developed Size Factor | Selection based on size factor exposure score | Using cap-weights | | | | | | |
| Value | FTSE Developed Value Factor | Selection based on value factor exposure score | as base, stocks weights are tilted by | Country and | | | | | |
| Mom. | FTSE Developed Momentum Factor | All stocks in CW parent index universe | their respective factor | industry constraints | | | | | |
| Low Vol. | FTSE Developed Volatility Factor | Selection based on volatility factor exposure score | scores. | | | | | | |
| | | FTSE RAFI Index Methodology | | | | | | | |
| Value | FTSE RAFI 1000 | Selection of 1000 stocks with the highest fundamental value from CW parent index | Stocks' weights are calculated based on their investable RAFI fundamental value composite score. | None | | | | | |

Absolute and relative performance

Exhibit 2 shows that all indices generally achieve outperformance over the broad cap-weighted index both in terms of returns and Sharpe ratio. This shows that the factor indices are able to benefit from the rewarded factor, some more than others. In the USA universe, Scientific Beta factor indices achieve the highest outperformance in each factor category. For example, the Scientific Beta USA Low Volatility Diversified Multi-Strategy index has excess returns of 2.70% compared to just 1.39% for the closest competitor and the Scientific Beta USA Value Diversified Multi-Strategy index has excess returns of 3.16% compared

to 2.38% for the closest competitor (Russell) and 1.94% for FTSE RAFI 1000 US.

We have seen that any portfolio tilted towards a rewarded risk factor will be rewarded by nature. This is why all Scientific Beta tilted CW indices, which make no effort to achieve diversification, have positive excess returns. The outperformance can sometimes be quite high, for example in the case of Mid-Cap indices (3.03% and 2.65% for US and Developed indices respectively), but it comes at the cost of higher volatility. Therefore, the role of diversification can truly be demonstrated by comparing risk-adjusted performance – the Sharpe

ratios. The Sharpe ratio of the Scientific Beta Mid-Cap indices is far higher than that of their tilted CW counterparts. In general, the Sharpe ratios of Scientific Beta indices are also invariably superior in each factor category.

Investing in a single factor comes at the risk of short-term relative losses, which can be large at times (Asness (1992) and Cohen, Polk and Vuolteenaho (2003)). Therefore, maximum relative drawdown becomes an important measure of risk. This is the maximum relative loss, compared to the CW benchmark, experienced by a strategy between a peak and a valley over a specified period. The results show that

¹³ The Scientific Beta USA (Developed) stock universe consists of 500 (2000) stocks, therefore each factor index is constructed on 250 (1000) stocks. The index construction methodology remains identical across regions.

¹⁴ While it is beyond the scope of this document to assess the implementation rules across providers, it is clear that factor indices potentially improve upon paper portfolios used to study factor premia in academic studies as far as investability is concerned.

Exhibit 2: Absolute and Relative Analytics of Factor Indices with respect to broad CW index in USA and Developed universe

The table compares the absolute and relative performance of the Scientific Beta Multi-strategy index for four factor tilts with the competing indices. Extreme Tracking Error (95%) is the 95th percentile of the distribution of 1-year rolling window tracking errors. Maximum relative drawdown is the maximum drawdown of the long/short index whose return is given by the fractional change in the ratio of the strategy index to the benchmark index. For USA (Developed), the S&P 500 index (the MSCI World index) is used as the benchmark. Yield on Secondary US Treasury Bills (3M) is used as a proxy for the risk-free rate. The analysis is based on daily total returns of indices in the period 01-Jan-2004 to 31-Dec-2013 (10 years).

| | | Absolute Analytics | | | | | Relative Analytics (benchmark = S&P 500) | | | |
|-------------------------------------|----------------|--------------------|-----------------|----------------|-----------------|--------------------|--|----------------------|---------------------------------------|-----------------------------|
| Panel A USA Factor Indices | Ann Returns | Ann Volatility | Sharpe Ratio | CF VaR (5%) | Max Drawdown | Ann Rel Returns | Ann Tracking Error | Information Ratio | Extreme (95%) Tracking Error | Max Relative Drawdown |
| S&P 500 Index | 7.38% | 20.37% | 0.29 | 1.77% | 55.25% | - | - | - | - | - |
| SciBeta Mid Cap CW | 10.41% | 22.33% | 0.40 | 2.08% | 57.09% | 3.03% | 5.38% | 0.56 | 9.18% | 18.95% |
| MSCI USA Equal Weighted | 9.51% | 22.70% | 0.35 | 2.07% | 59.77% | 2.13% | 4.45% | 0.48 | 10.12% | 17.04% |
| Russell Mid Cap | 10.19% | 22.61% | 0.38 | 2.12% | 58.93% | 2.81% | 5.08% | 0.55 | 9.31% | 17.80% |
| SciBeta Mid Cap Multi- Strategy | 10.80% | 20.29% | 0.45 | 1.87% | 53.42% | 3.42% | 4.56% | 0.75 | 7.92% | 9.64% |
| SciBeta Momentum CW | 8.64% | 20.38% | 0.35 | 1.70% | 50.81% | 1.26% | 4.63% | 0.27 | 9.21% | 13.77% |
| MSCI USA Momentum | 9.39% | 20.83% | 0.38 | 1.94% | 55.94% | 2.01% | 7.79% | 0.26 | 15.80% | 23.59% |
| Russell High Efficiency Momentum | 9.06% | 20.92% | 0.36 | 1.85% | 52.90% | 1.68% | 4.49% | 0.38 | 7.61% | 10.19% |
| SciBeta Momentum Multi- Strategy | 9.40% | 20.07% | 0.39 | 1.76% | 53.25% | 2.02% | 5.50% | 0.37 | 10.85% | 16.22% |
| SciBeta Low Volatility CW | 7.94% | 17.82% | 0.36 | 1.46% | 51.10% | 0.56% | 4.01% | 0.14 | 7.10% | 12.12% |
| MSCI USA Minimum Volatility | 8.77% | 16.91% | 0.43 | 1.48% | 46.61% | 1.39% | 5.20% | 0.27 | 8.39% | 12.83% |
| Russell High Efficiency Low Vol | 8.56% | 17.06% | 0.41 | 1.40% | 47.50% | 1.18% | 4.79% | 0.25 | 9.39% | 11.36% |
| SciBeta Low Vol Multi- Strategy | 10.08% | 16.99% | 0.50 | 1.45% | 48.31% | 2.70% | 5.20% | 0.52 | 9.67% | 8.79% |
| SciBeta Value CW | 7.56% | 22.46% | 0.27 | 2.03% | 60.01% | 0.18% | 3.94% | 0.05 | 8.03% | 14.56% |
| MSCI USA Value Weighted | 7.53% | 22.12% | 0.27 | 1.97% | 60.81% | 0.15% | 3.33% | 0.05 | 8.10% | 14.51% |
| Russell High Efficiency Value | 9.76% | 22.55% | 0.36 | 2.03% | 59.34% | 2.38% | 4.50% | 0.53 | 11.31% | 11.59% |
| FTSE RAFI 1000 US | 9.32% | 22.16% | 0.35 | 1.99% | 60.22% | 1.94% | 4.31% | 0.45 | 11.05% | 12.71% |
| SciBeta Value Multi-Strategy | 10.54% | 20.63% | 0.43 | 1.87% | 53.75% | 3.16% | 3.56% | 0.89 | 5.49% | 5.97% |

Scientific Beta indices, with the exception of the momentum index, experienced maximum relative drawdown in the range of 6% to 10% during the analysis period – distinctly lower than the MSCI and Russell factor indices. The effect of risk reduction through diversification is particularly clear in the case of Value indices. The diversification-based Scientific Beta factor index exhibits maximum relative drawdown of 5.97% and a Sharpe ratio of 0.43, in comparison with FTSE RAFI 1000 US, which has maximum relative drawdown of 12.71% and a Sharpe ratio of 0.35.

Panel B of Exhibit 2 presents the same analysis in the Developed World stock universe. In each factor category, both the excess returns and Sharpe ratio of Scientific Beta factor indices is higher than those of competitors. For example, the Scientific Beta Developed Mid-Cap (Low Volatility) Diversified Multi-Strategy index has a Sharpe ratio of 0.55 (0.65) compared to just 0.46

(0.56) for the closest competitor. Other observations from the USA universe, such as higher information ratio and lower maximum relative drawdown for Scientific Beta indices, remain qualitatively similar in the Developed universe.

Robustness checks

It is understood that a view of average performance over some time frame does not reveal certain useful information, such as performance in extreme market conditions and consistency in beating the benchmark. These measures are indicative of the robustness of the strategies. Therefore, we compute 'outperformance probability' and performance in the top and bottom 25% of the market. The probability of outperformance is defined as the empirical frequency of outperforming the cap-weighted reference index over a given investment horizon. This calculation allows one to distinguish

between strategies that are sensitive to the choice of period in achieving their performance and those that are less so. For conditional analysis, performance in the top and bottom 25% quarters is analysed by CW index returns.

The outperformance probability of Scientific Beta indices is higher in the case of Size, Low Volatility and Value indices in both the USA and Developed universes. MSCI Value indices display around 25%-40% outperformance probability for a 3-year horizon, while for Scientific Beta indices this figure is around 90%. Except for USA momentum, all Scientific Beta factor indices achieve 100% outperformance probability for a 5-year investment horizon, meaning that if one invests in the strategy for a 5-year period (as factors perform over longer time frames), one would be sure to outperform the CW benchmark, irrespective of the entry time.

The information on extreme markets (25% bull vs. 25% bear) shows that the

| | Returns | voiatility | Rallo | (5%) | Diawdown | Returns | Error | Rallo | Error | Drawdown |
|---|---------|------------|-------|-------|----------|---------|-------|-------|--------|----------|
| MSCI World Index | 7.53% | 17.52% | 0.34 | 1.63% | 57.46% | - | - | - | - | - |
| SciBeta Mid Cap CW | 10.18% | 17.80% | 0.48 | 1.74% | 58.11% | 2.65% | 3.53% | 0.75 | 5.99% | 10.44% |
| MSCI World Equal Weighted | 9.22% | 17.44% | 0.44 | 1.71% | 59.66% | 1.70% | 4.47% | 0.38 | 8.37% | 13.40% |
| Russell Developed Small Cap | 9.14% | 17.41% | 0.43 | 1.79% | 60.64% | 1.61% | 5.95% | 0.27 | 11.50% | 17.95% |
| FTSE Developed Size Factor Index | 9.41% | 16.92% | 0.46 | 1.69% | 59.18% | 1.88% | 4.90% | 0.38 | 9.24% | 13.48% |
| SciBeta Mid Cap Multi- Strategy | 10.45% | 16.12% | 0.55 | 1.57% | 54.57% | 2.92% | 3.57% | 0.82 | 6.80% | 6.62% |
| SciBeta Momentum CW | 8.90% | 17.23% | 0.43 | 1.56% | 54.85% | 1.37% | 3.61% | 0.38 | 6.70% | 9.87% |
| MSCI World Momentum | 10.80% | 17.75% | 0.52 | 1.67% | 55.53% | 3.27% | 7.85% | 0.42 | 15.67% | 20.87% |
| Russell Dev HE LC Momentum | 10.22% | 18.24% | 0.47 | 1.71% | 56.69% | 2.69% | 3.99% | 0.68 | 5.98% | 9.97% |
| FTSE Dev Momentum Factor Index | 8.29% | 17.24% | 0.39 | 1.59% | 55.50% | 0.76% | 1.15% | 0.66 | 1.78% | 3.18% |
| SciBeta Momentum Multi- Strategy | 10.30% | 16.09% | 0.54 | 1.51% | 54.35% | 2.77% | 4.23% | 0.65 | 8.24% | 12.65% |
| SciBeta Low Volatility CW | 8.67% | 15.07% | 0.47 | 1.37% | 52.59% | 1.14% | 3.48% | 0.33 | 6.23% | 9.54% |
| MSCI World Minimum Volatility | 8.36% | 12.67% | 0.54 | 1.19% | 47.35% | 0.83% | 6.54% | 0.13 | 10.95% | 17.42% |
| Russell Dev HE Large Cap Low Vol | 9.52% | 14.09% | 0.56 | 1.28% | 49.60% | 1.99% | 4.75% | 0.42 | 8.95% | 13.16% |
| FTSE Dev Volatility Factor Index | 8.85% | 15.98% | 0.46 | 1.42% | 52.44% | 1.32% | 3.20% | 0.41 | 5.34% | 9.89% |
| SciBeta Low Vol Multi- Strategy | 10.54% | 13.79% | 0.65 | 1.30% | 49.55% | 3.01% | 4.79% | 0.63 | 9.24% | 9.76% |
| SciBeta Value CW | 7.82% | 18.80% | 0.33 | 1.76% | 60.07% | 0.29% | 2.61% | 0.11 | 4.83% | 11.03% |
| MSCI World Value Weighted | 7.53% | 18.61% | 0.32 | 1.75% | 61.55% | 0.00% | 2.73% | 0.00 | 5.82% | 11.51% |
| Russell Dev HE Large Cap Value | 9.70% | 18.61% | 0.44 | 1.77% | 61.61% | 2.17% | 3.87% | 0.56 | 8.71% | 12.24% |
| FTSE Dev Value Factor Index | 8.16% | 18.74% | 0.35 | 1.76% | 60.47% | 0.64% | 3.52% | 0.18 | 7.79% | 12.03% |
| FTSE RAFI 1000 Developed | 8.46% | 19.15% | 0.36 | 1.79% | 61.00% | 0.93% | 3.92% | 0.24 | 9.11% | 13.50% |
| SciBeta Value Multi-Strategy | 10.21% | 17.23% | 0.50 | 1.66% | 57.32% | 2.68% | 2.55% | 1.05 | 4.19% | 5.68% |
| dependence of the performance of allis not disclosed by all the other index | | | | | | | | | | |

CF VaR

Max

Ratio (5%) Drawdown Returns

Ann Rel

Tracking

dependence of the performance of all indices on market conditions is quite high. Relative to the broad CW index, Size and Value indices are favoured in bull markets, while Momentum and Low Volatility indices perform better in bear markets. It is sometimes argued therefore that a combination of factor indices is better suited for an investor who desires more consistent outperformance across market cycles.

Panel B

Developed Factor Indices

Our results show that factor indices in general deliver attractive performance, as they take advantage of risk factors that are supported by academic research. However, Scientific Beta's methodology, aiming at improved diversification within the factor space, provides better extraction of the related risk premia. Caution is in order when assessing any performance comparison that is based on a limited time period. That is why ERI Scientific Beta calculates long-term track records over 40 years on US data. Since the equivalent of these calculations

is not disclosed by all the other index providers, it has not been possible to make this comparison. In fact, a key question that any index provider faces is potential criticism that indices could be a result of a data mining exercise, which in turn implies that performance may not be robust. Therefore, in addition to performance numbers, a key question is the methodological robustness of the different offerings. For index performance to be considered robust, index providers should follow transparent and consistent methodologies and build their indices on consensual factor definitions and models, which is unfortunately not always the case. as we show here. Therefore, beyond assessing the performance of backtests, the methodological robustness is likely to become a key consideration for investors going forward. ■

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Relative Analytics (benchmark = MSCI World)

Ratio

Tracking

Relative

References

- Amenc, N., F. Goltz and L. Martellini. 2013.
 Smart Beta 2.0. EDHEC-Risk Institute
 Position Paper.
- Asness, C. 1992. Changing Equity Risk Premia and Changing Betas over the Business Cycle and January. University of Chicago Working Paper.
- Bender, J., R. Briand, D. Melas, R. Subramanian and M. Subramanian.
 Deploying Multi-Factor Index Allocations in Institutional Portfolios. MSCI White Paper, 2013.
- Cohen, R. B., C. Polk and T. Vuolteenaho. 2003. The Value Spread. *Journal of Finance* 58(2): 609-642.

Exhibit 3: Robustness Analytics of Factor Indices in USA and Developed universes

The table compares the robustness and conditional performance of the Scientific Beta Multi-strategy index for four factor tilts with the competing indices. Outperformance Probability is the probability of obtaining positive excess returns over CW if one invests in the strategy at any point in time for a period of 3 (or 5) years. It is computed as the frequency of positive values in the series of excess returns assessed over a rolling window of 3 (or 5) years and step size of one week covering the entire investment horizon. The top 25% of quarters with highest market returns are considered extremely bullish and the bottom 25% quarters with the lowest returns are considered extremely bearish. For USA (Developed), the S&P 500 index (the MSCI World index) is used as the benchmark. Yield on Secondary US Treasury Bills (3M) is used as a proxy for the risk-free rate. The analysis is based on daily total returns of indices in the period 01-Jan-2004 to 31-Dec-2013 (10 years).

| Panel A | Outperformar | nce Probability | Extreme Bull | (25% best) | Extreme Bear (25% worst) | | |
|----------------------------------|--------------|-----------------|----------------|----------------|--------------------------|----------------|--|
| USA Factor Indices | 3-Year | 5-Year | Excess Returns | Tracking Error | Excess Returns | Tracking Error | |
| SciBeta Mid Cap CW | 84% | 98% | 7.19% | 4.18% | -1.34% | 7.51% | |
| MSCI USA Equal Weighted | 85% | 98% | 11.82% | 4.68% | -3.00% | 6.44% | |
| Russell Mid Cap | 86% | 100% | 11.43% | 4.76% | -2.53% | 7.00% | |
| SciBeta Mid Cap Multi-Strategy | 95% | 100% | 1.06% | 3.84% | 3.04% | 6.16% | |
| SciBeta Momentum CW | 56% | 76% | -2.93% | 3.59% | 2.93% | 6.82% | |
| MSCI USA Momentum | 58% | 57% | 1.28% | 5.65% | 2.45% | 11.70% | |
| Russell High Efficiency Momentum | 91% | 94% | 2.51% | 3.64% | 0.03% | 6.35% | |
| SciBeta Momentum Multi-Strategy | 60% | 68% | -3.27% | 4.36% | 2.46% | 8.21% | |
| SciBeta Low Volatility CW | 64% | 71% | -6.91% | 4.13% | 5.47% | 5.53% | |
| MSCI USA Minimum Volatility | 87% | 94% | -9.12% | 5.16% | 10.98% | 7.20% | |
| Russell High Efficiency Low Vol | 78% | 97% | -8.69% | 4.48% | 8.04% | 6.98% | |
| SciBeta Low Vol Multi-Strategy | 100% | 100% | -7.15% | 4.97% | 8.79% | 7.48% | |
| SciBeta Value CW | 28% | 17% | 3.80% | 3.82% | -3.30% | 5.81% | |
| MSCI USA Value Weighted | 39% | 21% | 6.96% | 3.46% | -3.53% | 5.29% | |
| Russell High Efficiency Value | 88% | 100% | 11.37% | 4.99% | -1.14% | 6.62% | |
| FTSE RAFI 1000 US | 82% | 95% | 15.17% | 6.24% | -3.05% | 4.65% | |
| SciBeta Value Multi-Strategy | 92% | 100% | 1.72% | 2.90% | 2.72% | 4.54% | |

| 37 | I | | 1 | | ' | |
|----------------------------------|--------------|-----------------|----------------|----------------|----------------|----------------|
| Panel B | Outperformar | nce Probability | Extreme Bull | (25% best) | Extreme Bear | (25% worst) |
| Developed Factor Indices | 3-Year | 5-Year | Excess Returns | Tracking Error | Excess Returns | Tracking Error |
| SciBeta Mid Cap CW | 80% | 100% | 6.12% | 2.70% | 0.21% | 4.93% |
| MSCI World Equal Weighted | 67% | 99% | 9.48% | 3.53% | -0.98% | 6.22% |
| Russell Developed Small Cap | 61% | 88% | 13.96% | 4.57% | -1.73% | 8.52% |
| FTSE Developed Size Factor Index | 74% | 98% | 8.39% | 3.78% | -1.37% | 7.10% |
| SciBeta Mid Cap Multi-Strategy | 97% | 100% | 0.80% | 3.19% | 4.14% | 5.06% |
| SciBeta Momentum CW | 76% | 79% | -1.47% | 3.04% | 1.76% | 5.11% |
| MSCI World Momentum | 63% | 82% | -3.90% | 5.81% | 5.61% | 11.50% |
| Russell Dev HE LC Momentum | 86% | 100% | 3.94% | 3.15% | 0.30% | 5.31% |
| FTSE Dev Momentum Factor Index | 100% | 100% | -0.74% | 0.95% | 1.67% | 1.61% |
| SciBeta Momentum Multi-Strategy | 80% | 100% | -1.00% | 3.89% | 3.58% | 5.95% |
| SciBeta Low Volatility CW | 81% | 97% | -6.92% | 3.09% | 5.72% | 4.80% |
| MSCI World Minimum Volatility | 75% | 93% | -13.19% | 5.42% | 12.85% | 9.20% |
| Russell Dev HE Large Cap Low Vol | 93% | 96% | -8.52% | 4.22% | 8.75% | 6.69% |
| FTSE Dev Volatility Factor Index | 89% | 97% | -6.99% | 2.61% | 6.06% | 4.27% |
| SciBeta Low Vol Multi-Strategy | 100% | 100% | -6.49% | 4.09% | 8.87% | 6.93% |
| SciBeta Value CW | 29% | 34% | 3.03% | 2.29% | -2.34% | 3.67% |
| MSCI World Value Weighted | 25% | 20% | 5.61% | 2.50% | -3.04% | 3.99% |
| Russell Dev HE Large Cap Value | 68% | 95% | 10.88% | 4.00% | -1.82% | 5.57% |
| FTSE Dev Value Factor Index | 33% | 47% | 4.42% | 2.64% | -2.55% | 5.44% |
| FTSE RAFI 1000 Developed | 70% | 74% | 11.26% | 5.04% | -3.12% | 4.71% |
| SciBeta Value Multi-Strategy | 88% | 100% | 3.65% | 1.98% | 1.45% | 3.42% |

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LIVE IS BETTER

Since they are based most often on systematic and transparent weighting rules, smart beta indices can provide simulated long-term historical track records.

Nonetheless, however long the historical track record might be, it can always be questioned. The rebalancing rules or the choice of factors for the smart beta indices may have been chosen to optimise the in-sample performance.

Relying on academic consensus for factor definitions and weighting methods, the Scientific Beta indices that are drawn from EDHEC-Risk Institute's research want to avoid these robustness problems.

It's not surprising therefore that the live track records of our Scientific Beta Multi-Beta Multi-Strategy indices are as good as the simulated track records*.

18% improvement in relative performance with an average annualised outperformance of 3.49% compared to the reference cap-weighted index.

94% improvement in information ratio relative to the reference cap-weighted index with an annualised average of 1.33.

For more information, please visit www.scientificbeta.com or contact Mélanie Ruiz on +33 493 187 851 or by e-mail to melanie.ruiz@scientificbeta.com



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* Evaluation conducted on live track record period beginning on December 20, 2013, for Equal-Weight (EW)-allocation Scientific Beta Multi-Beta Multi-Strategy indices and Equal Risk Contribution (ERC)-allocation Scientific Beta Multi-Beta Multi-Strategy indices for all developed world regions, compared to the simulated track records for the same Scientific Beta indices with an inception date of June 21, 2002, for the EW allocation and December 19, 2003, for the ERC allocation, with calculations up to December 31, 2014. For the period since inception (June 21, 2002 to December 31, 2014), the average annualised excess return of these Scientific Beta indices compared to the reference cap-weighted index is 2.95% (information based on historical simulation). Source: www.scientificbeta.com. Information containing any historical information, data or analysis should not be taken as an indication or guarantee of any future performance, analysis, forecast or prediction. Past performance does not guarantee future results.